Physical Properties of $s_{\pm}$ Superconductors as a Model of Iron Pnictides

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In collaboration with

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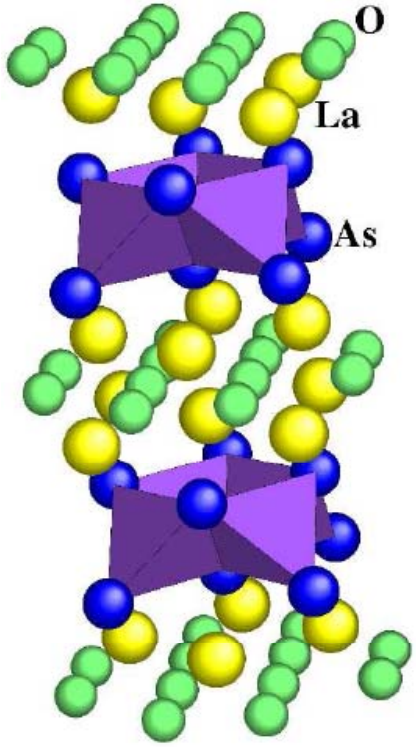
Y. Tanaka, Nagoya University, Japan

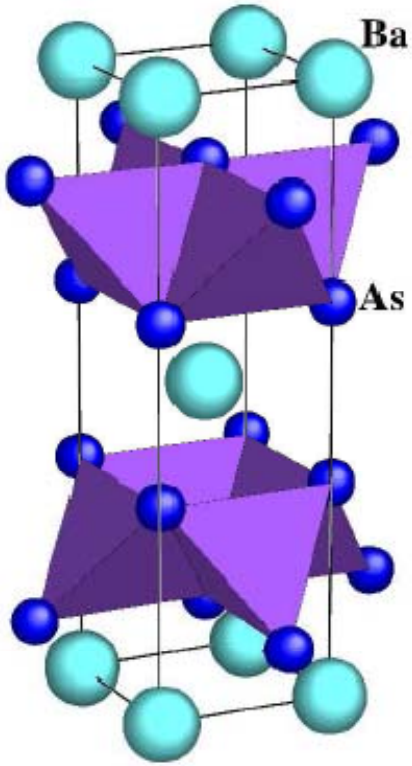
Outline

- Introduction.
- Robustness of $s_{\pm}$ pairing against impurities.
- Absence of the *Hebel-Slichter* peak in NMR relaxation and *T*-dependence of $1/T_1$.
- Gaps and electromagnetic response in the $s_{\pm}$ model
- Tunneling in the $s_{\pm}$ model

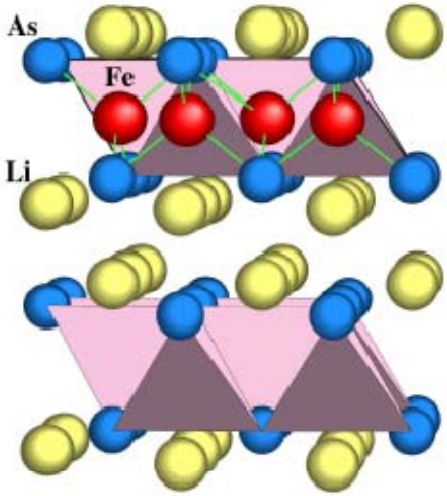
Crystal structure of FeAs superconductors



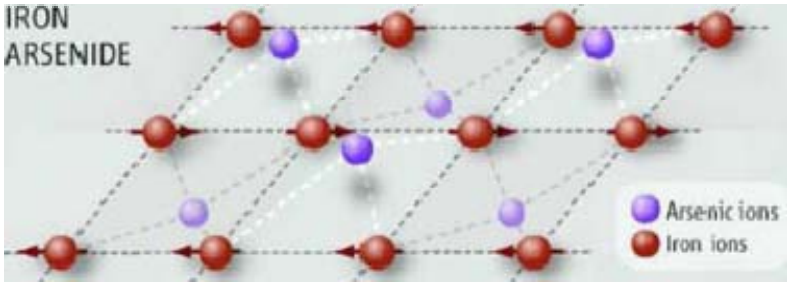
LaOFeAs



$BaFe_2As_2$



LiFeAs



FeAs tetrahedra form two-dimensional layers surrounded by LaO, Ba or Li.
Fe ions inside tetrahedra form a square lattice.

Basic Experiments on FeAs

February 2008

J|A|C|S COMMUNICATIONS

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Iron-Based Layered Superconductor La[$O_{1-x}F_x$]FeAs (x = 0.05–0.12) with T_c = 26 K

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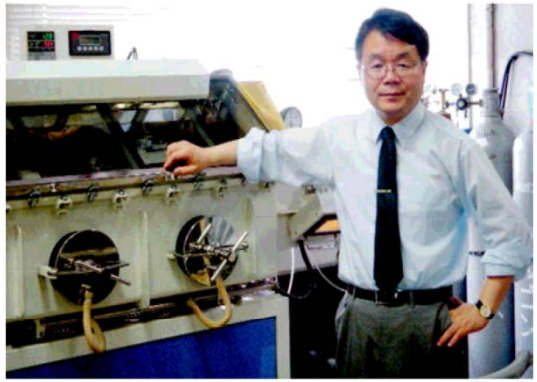
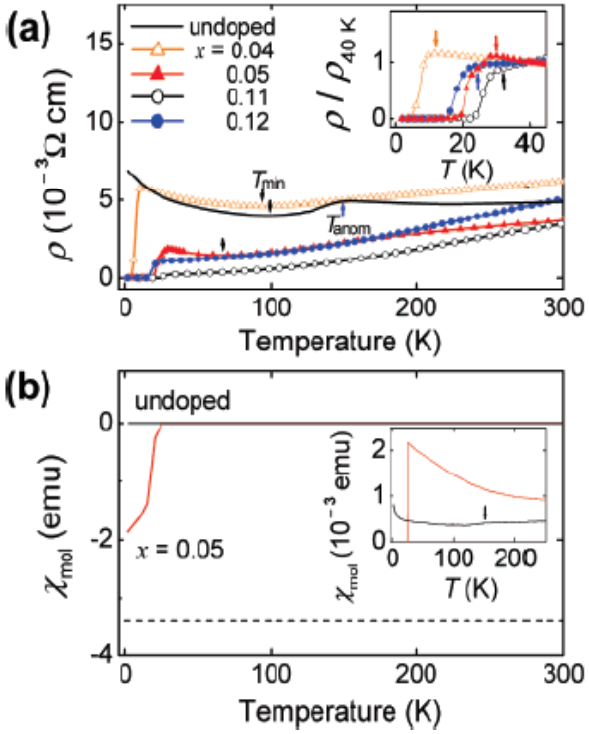
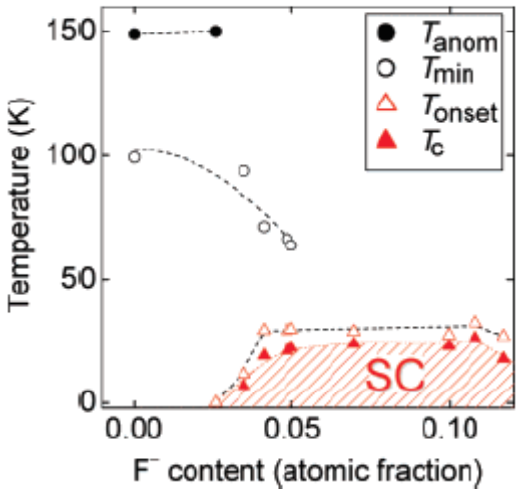
ERATO-SORST, JST, Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, Materials and Structures Laboratory, Tokyo Institute of Technology, Mail Box R3-1, and Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, 4259 Nagatsuta, Midori-ku, Yokohama 226-8503, Japan

Received January 9, 2008; E-mail: hosono@msl.titech.ac.jp

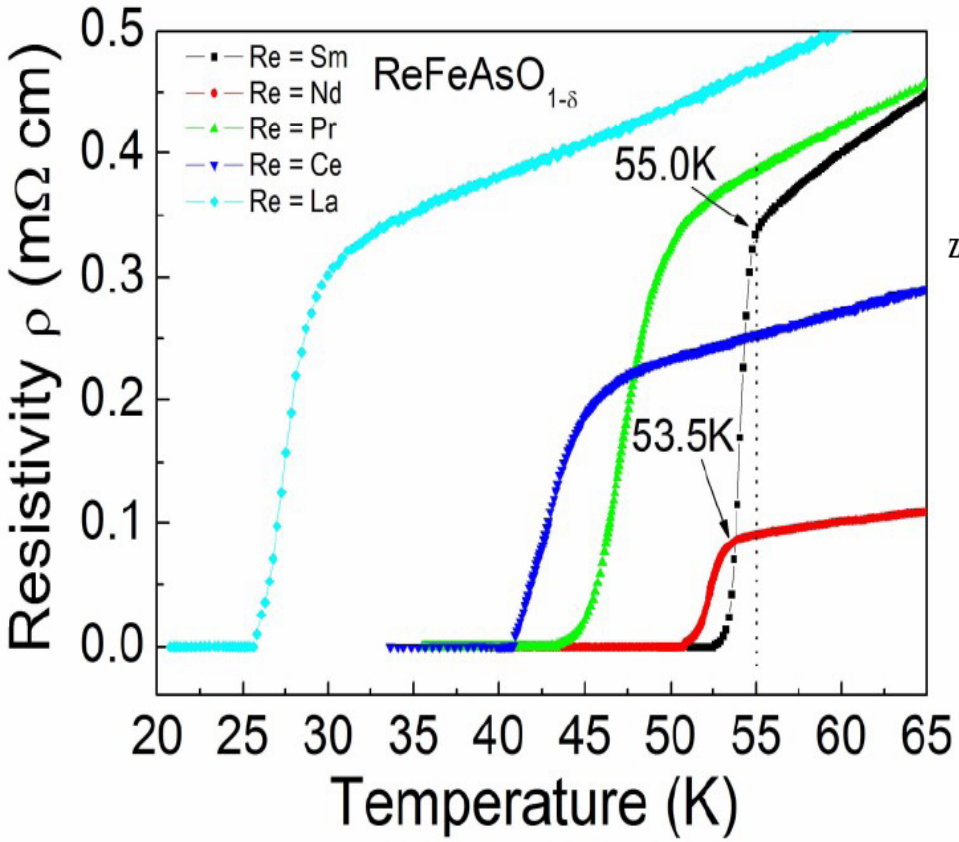
■ J. AM. CHEM. SOC. 2008, *130*, 3296–3297







Electron doping!



Superconductivity and Phase Diagram in Iron-based Arsenic-oxides $ReFeAsO_{1-\delta}$ (Re = rare earth metal) without Fluorine Doping

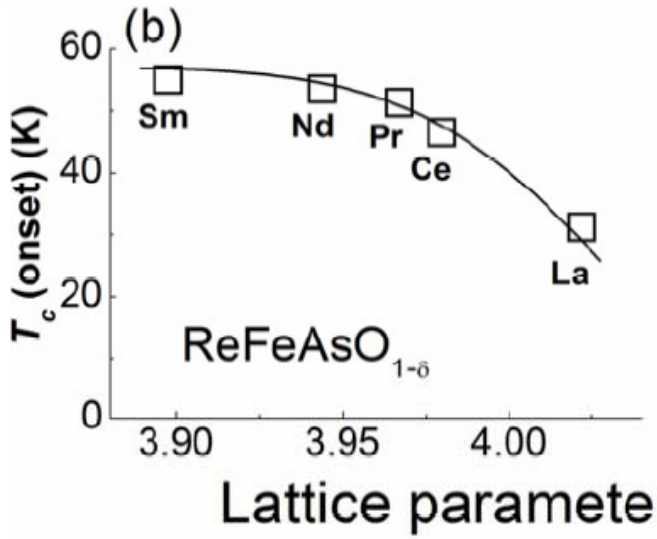
Zhi-An Ren*, Guang-Can Che, Xiao-Li Dong, Jie Yang, Wei Lu, Wei Yi, Xiao-Li Shen, Zheng-Cai Li, Li-Ling Sun, Fang Zhou, Zhong-Xian Zhao*

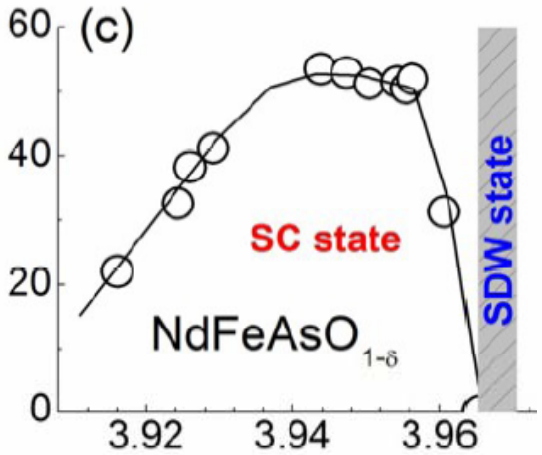
Europhysics Letters, 83 (2008) 17002

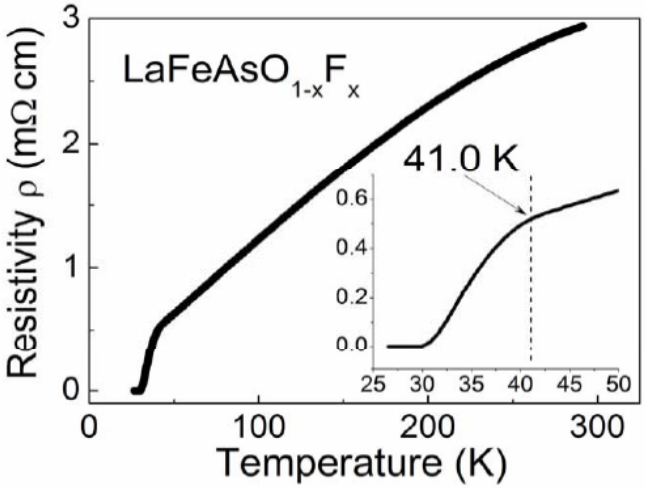
Superconductivity at 41.0 K in the F-doped $LaFeAsO_{1-x}F_x$

Wei Lu, Xiao-Li Shen, Jie Yang, Zheng-Cai Li, Wei Yi, Zhi-An Ren*, Xiao-Li Dong, Guang-Can Che, Li-Ling Sun, Fang Zhou, Zhong-Xian Zhao*

arXiv: 0804.3725







Tc in ReOFeAS series

Table 1.

Re	a (Å)	c (Å)	T_c (onset-R) (K)	T_c (zero-R) (K)	T_c (onset-M) (K)
Sm (HP)	3.897(6)	8.407(1)	55.0	52.8	55.0
Sm (AP)	3.933(5)	8.495(3)			
Nd (HP)	3.943(7)	8.521(8)	53.5	50.9	51.0
Nd (AP)	3.965(3)	8.572(3)			
Pr (HP)	3.968(2)	8.566(1)	51.3	43.2	48.2
Pr (AP)	3.985(8)	8.600(3)			
Ce (HP)	3.979(7)	8.605(5)	46.5	41.0	42.6
Ce (AP)	3.998(1)	8.652(6)			
La (HP)	4.022(2)	8.707(1)	31.2	25.9	28.3
La (AP)	4.033(5)	8.739(1)			

Note: The HP samples are for the nominal composition of $ReFeAsO_{0.85}$, and the AP samples are for the nominal composition of ReFeAsO. And here we also note that T_c(onset) ~ 36 K in $LaFeAsO_{1-\delta}$ has been achieved by HP synthesis but the sample quality is still not good enough.

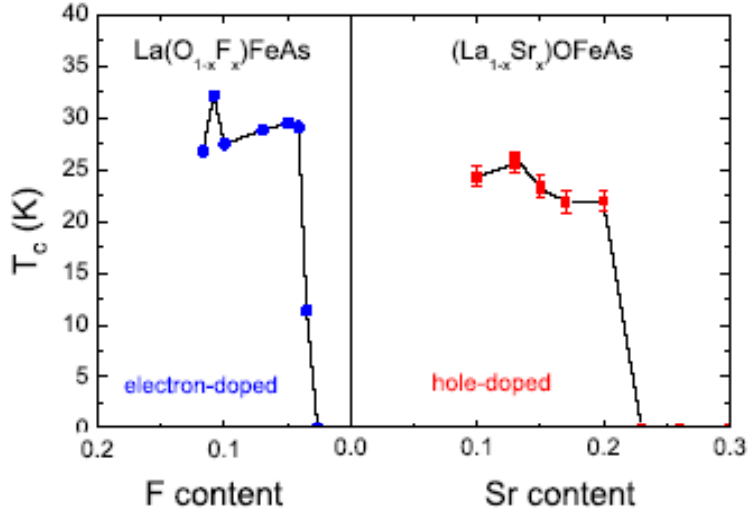
arXiv:
0804.2582

Journal of the Physical Society of Japan
Vol. 77, No. 6, June, 2008, 063707

Superconductivity at 25 K in hole doped $(La_{1-x}Sr_x)OFeAs$

Hai-Hu Wen*, Gang Mu, Lei Fang, Huan Yang, and Xiyu Zhu

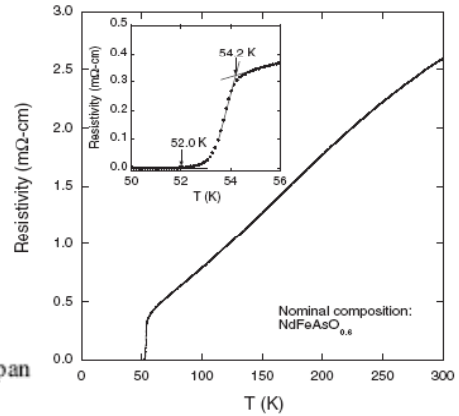
Europhys. Lett. 82, 17009 (2008)

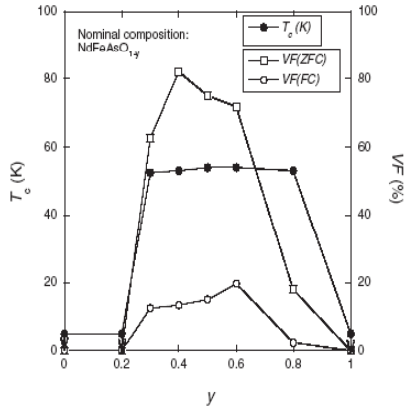


Superconductivity at 54 K in F-Free $NdFeAsO_{1-y}$

Hijiri Kito, Hiroshi Eisaki, and Akira Iyo*

Nanoelectronics Research Institute (NeRI), National Institute of Advanced Industrial Science and Technology (AIST), 1-1-1 Central 2, Umezono, Tsukuba, Ibaraki 305-8568

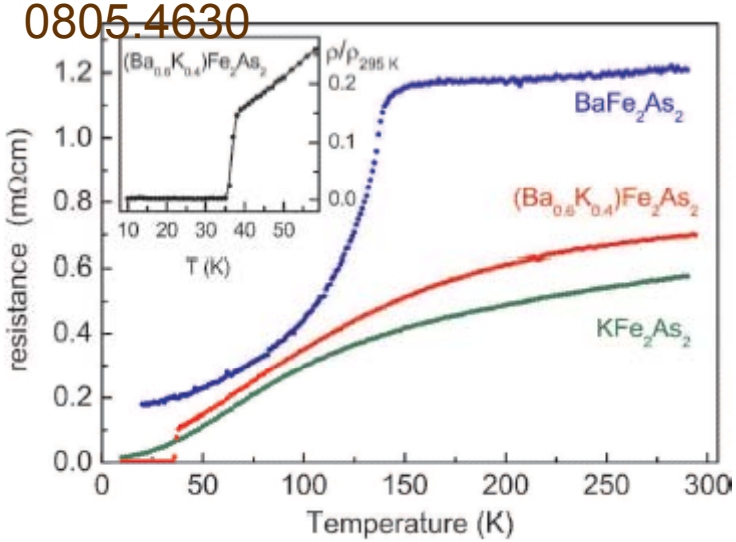


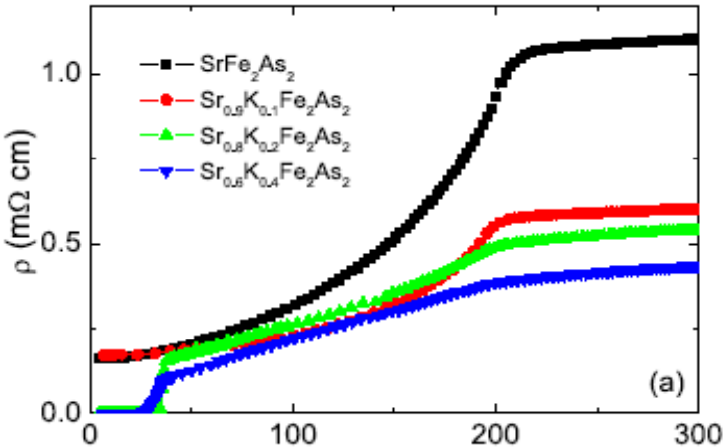


Superconductivity at 38 K in the iron arsenide $(Ba_{1-x}K_x)Fe_2As_2$

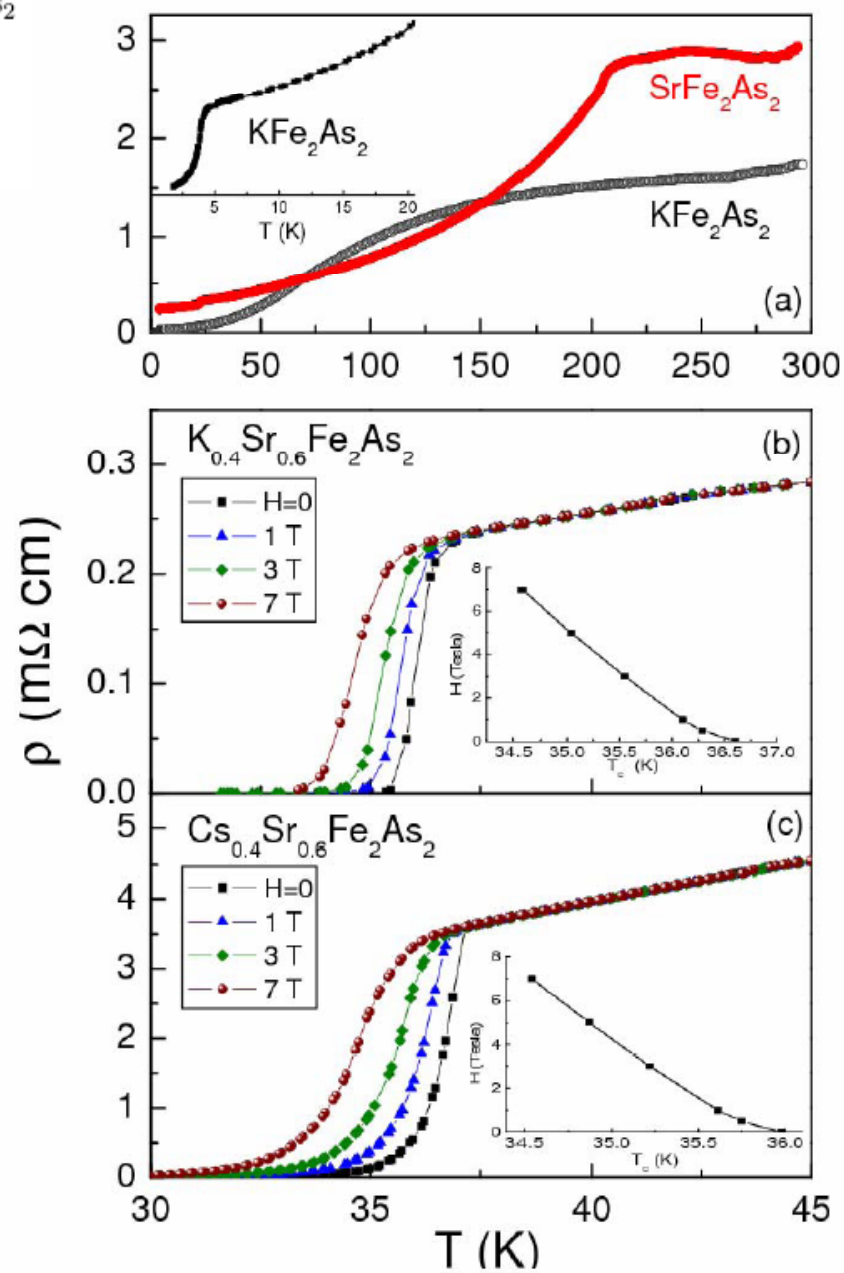
Marianne Rotter, Marcus Tegel and Dirk Johrendt*
Department Chemie und Biochemie, Ludwig-Maximilians-Universität München, Butenandtstrasse 5-13 (Haus D), 81377 München, Germany
(Dated: May 29, 2008)

arXiv:
0805.4630



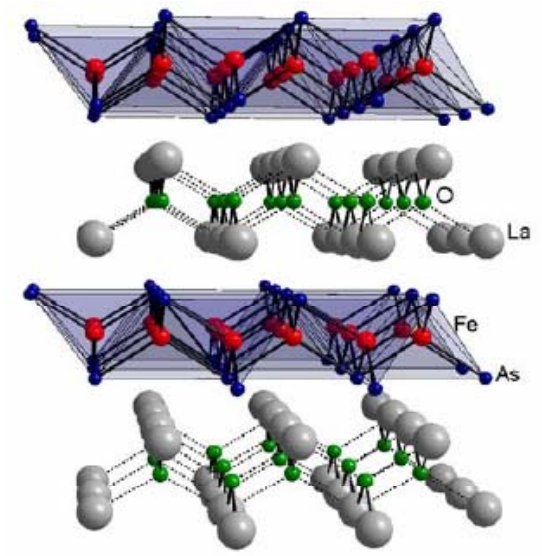


G.F.Chen et al. arXiv: 0806.1209

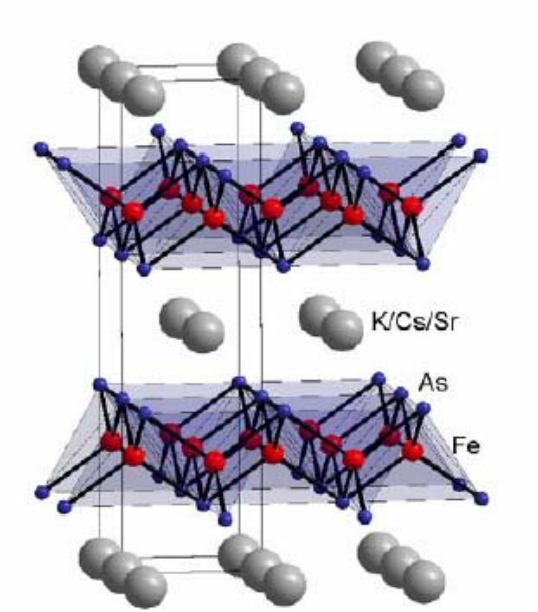


K.Sasmai et al. (C.W.Chu) arXiv: 0806.1

Basic crystal structure of FeAs superconductors

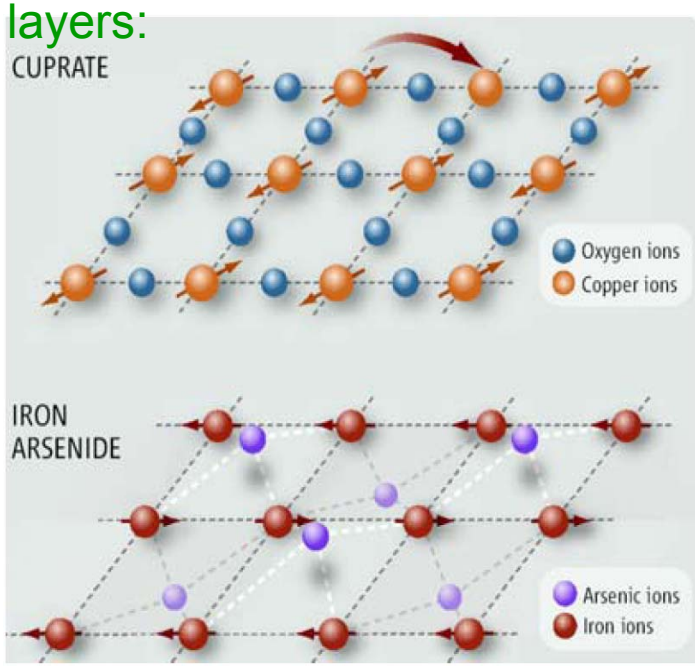


$$(\mathrm{RE})^{+3}\mathrm{O}^{-2}\mathrm{Fe}^{+2}\mathrm{As}^{-3}$$



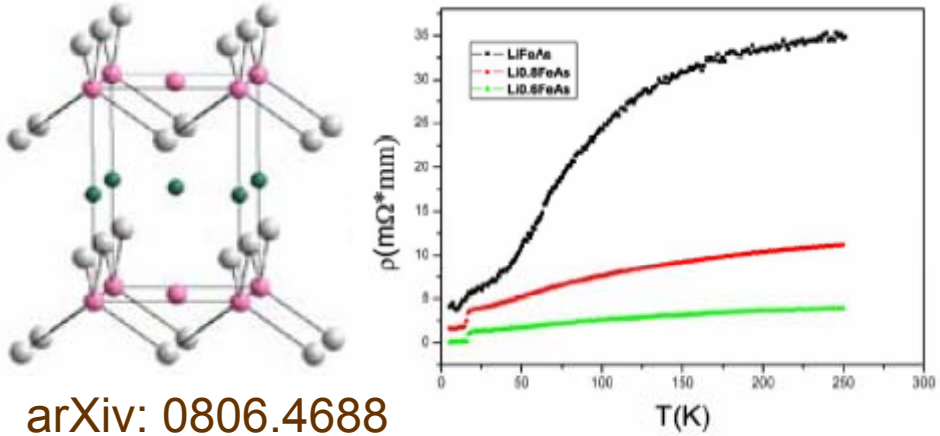
$$Ba^{+2}(Fe^{+2})_2(As^{-3})_2$$

CuO_2 as compared with FeAs layers:



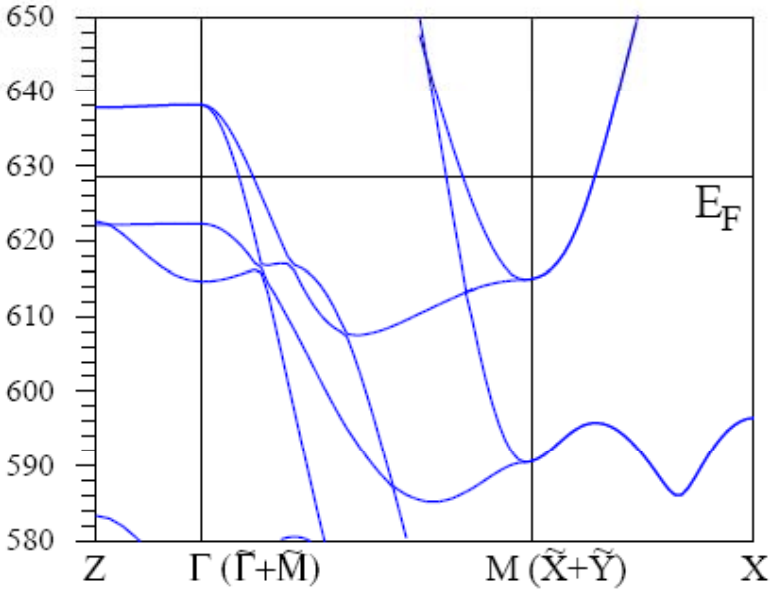
The superconductivity at 18 K in $Li_{1-x}FeAs$ compounds

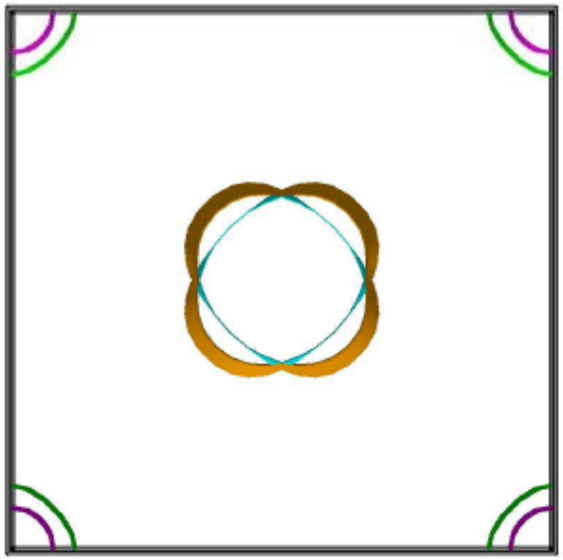
X.C.Wang, Q.Q. Liu, Y.X. Lv, W.B. Gao, L.X.Yang, R.C. Yu, F.Y.Li, C.Q. Jin*



arXiv: 0806.4688

Band structure



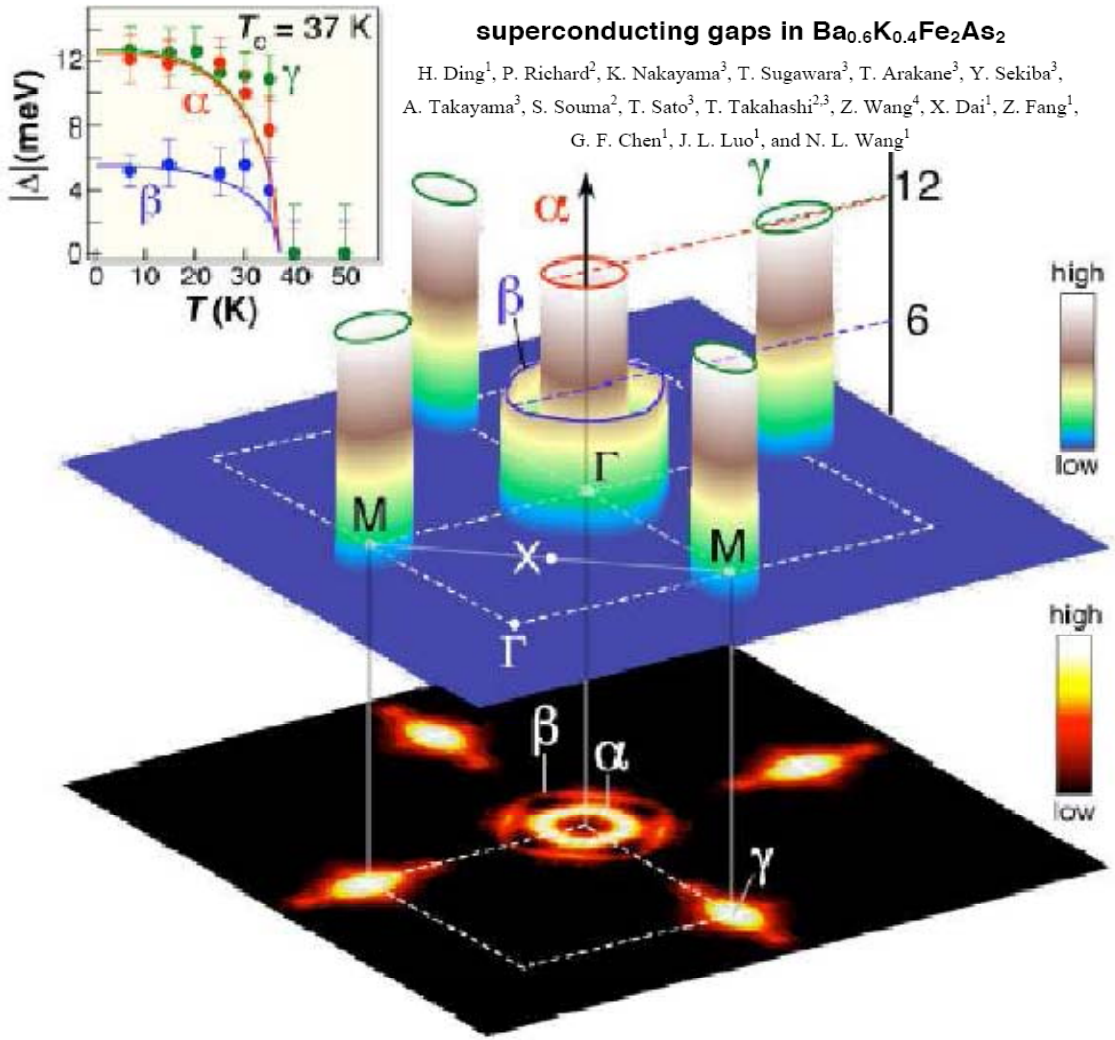


Superconducting gap – ARPES data

Observation of Fermi-surface-dependent nodeless superconducting gaps in $Ba_{0.6}K_{0.4}Fe_2As_2$

H. Ding[1], P. Richard[2], K. Nakayama[3], T. Sugawara[3], T. Arakane[3], Y. Sekiba[3], A. Takayama[3], S. Souma[2], T. Sato[3], T. Takahashi[2,3], Z. Wang[4], X. Dai[1], Z. Fang[1], G. F. Chen[1], J. L. Luo[1], and N. L. Wang[1]

arXiv: 0807.0419



Schematic picture of superconducting gaps in $Ba_{0.6}K_{0.4}Fe_2As_2$. Lower picture represents Fermi surfaces (ARPES intensity), upper insert – temperature dependence of gaps at different Sheets of the Fermi surface.

Spin fluctuations

$$\chi(\mathbf{q},\omega) = \frac{\chi_0(\mathbf{q},\omega)}{1 - J(\mathbf{q},\omega)\ \chi_0(\mathbf{q},\omega)}$$

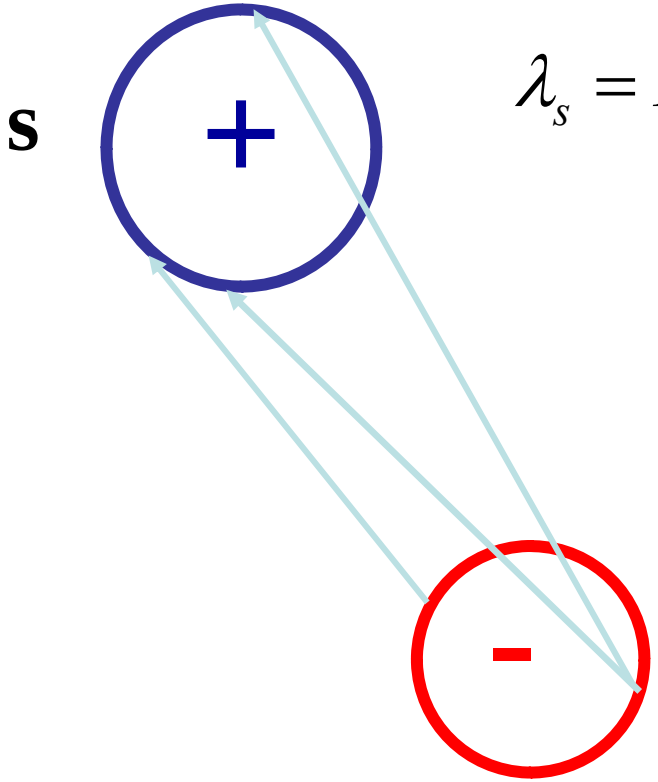
For a Mott-Hubbard system, $J(\mathbf{q},\omega)$ -magnetic interaction is *local in real space*

$$\chi_0(\mathbf{q},\omega) = \sum_{\mathbf{k}} \frac{f(\varepsilon_{\mathbf{k}+\mathbf{q}}) - f(\varepsilon_{\mathbf{k}})}{(\varepsilon_{\mathbf{k}+\mathbf{q}} - \varepsilon_{\mathbf{k}} - \omega - i\delta)}$$

the <u>*s/c*</u> physics is just the same as old Berk-Schrieffer physics

1) Interaction is repulsive and peaked at $(\pi,\pi) \rightarrow$ pairing in $s\pm$ channel
2) Mass renormalization expected up to the energy of spin fluctuations

Repulsive pairing interactions in the $s_{+/-}$ channel:



$$\lambda_s = N(0)\left\langle\left\langle V(\mathbf{q})\right\rangle\right\rangle_{\mathrm{FS}}$$

<u>s-wave:</u>
V>0 for all **q**

SF exchange repulsive, but pairing for all q's!

NB: ANY magnetic interaction with this structure works in the same way, whether χ_0-driven or J-driven, whether linear or nonlinear…

Some properties of the $s_{+/-}$ state

1. Thermodynamics is exponential in clean limit (weak coupling)
   C/T, penetration depth, NMR $1/TT_1$. Singlet K
2. Reversed role of magnetic/nonmagnetic interband impurity scattering
   See next slides
3. Coherence factors: depend on the probing wave vector, BCS at $q \approx 0$, anti-BCS at $q \approx (\pi,\pi)$.
   - *suppressed Hebel-Slichter peak*
   suppressed Hebel-Slichter peak
4. Andreev bound states at finite energies
   See next slides
5. Enhancement of spin susceptibility near $q \approx (\pi,\pi)$ below T_c
   observed
7. Full gap(s) in tunneling
   Full gap(s) in Andreev and in ARPES

Experiments: symmetry of the superconducting order parameter

Fully gapped superconducting state:

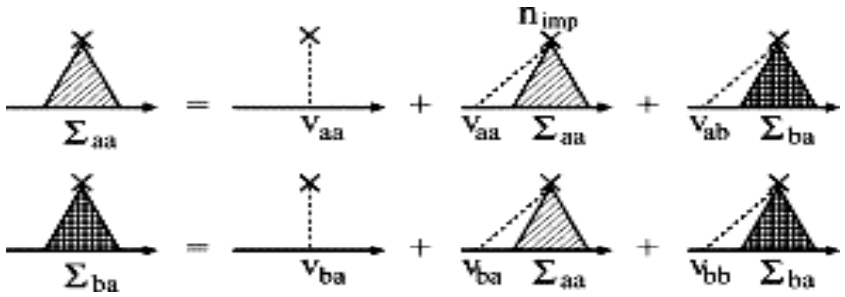
- PCAR: Y.Y. Chen et al., Nature 453, 1224 (2008); K.A. Yates et al., Supercond. Sci. Technol. 21, 092003 (2008); R.S. Gonnelli et al., arXiv:0807.3149.
- ARPES: L. Zhao et al., arXiv:0807.0398; H. Ding et al., EPL 83, 47001 (2008); T. Kondo et al., arXiv:0807.0815.
- Penetration depth: C. Martin et al., arXiv:0807.0876; K. Hashimoto et al., arXiv:0806.3149; L. Malone et al., arXiv:0806.3908

NMR – Lines of nodes at the FS:

- ^{75}As NMR: $1/T_1$ with a T^3 behavior below T_c (line of nodes?)
  Y. Nakai et al., JPSJ 77, 073701 (2008)
- ^{19}F NMR: $1/T_1$ can be explained by a two d-wave gap scenario, $\Delta=\Delta_1+\Delta_2$, $\Delta_1=3.5\ k_BT_c$, $\Delta_2=1.1k_BT_c$
  K. Matano et al., EPL 83, 57001 (2008)

Effect of impurities

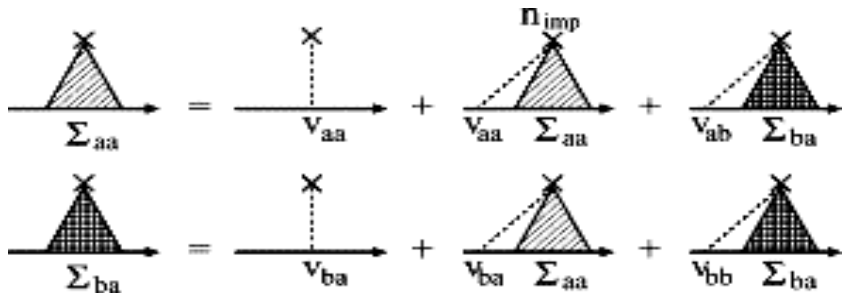
$$\hat{G} = \hat{G}_0 - \hat{\Sigma}_{imp}$$



Effect of impurities

$$\hat{G} = \hat{G}_0 - \hat{\Sigma}_{imp}$$

$$\hat{v} = \begin{pmatrix} 0 & v \\ v & 0 \end{pmatrix}$$



Interband impurities

$$\Sigma_{aa}^{(0)} = -i\gamma_a \frac{\sigma\bar{\omega}_{an}\sqrt{\bar{\Delta}_{bn}^2 + \bar{\omega}_{bn}^2} - (\sigma - 1)\,\bar{\omega}_{bn}\sqrt{\bar{\Delta}_{an}^2 + \bar{\omega}_{an}^2}}{\det a}$$

$$\Sigma_{aa}^{(1)} = \gamma_a \frac{\sigma\bar{\Delta}_{an}\sqrt{\bar{\Delta}_{bn}^2 + \bar{\omega}_{bn}^2} + (\sigma - 1)\,\bar{\Delta}_{bn}\sqrt{\bar{\Delta}_{an}^2 + \bar{\omega}_{an}^2}}{\det a},$$

where $\gamma_i = \frac{n_{imp}\sigma}{\pi N_i(0)}$, and $\sigma = \frac{\pi^2 N_a(0) N_b(0) u^2}{1+\pi^2 N_a(0) N_b(0) u^2}$.

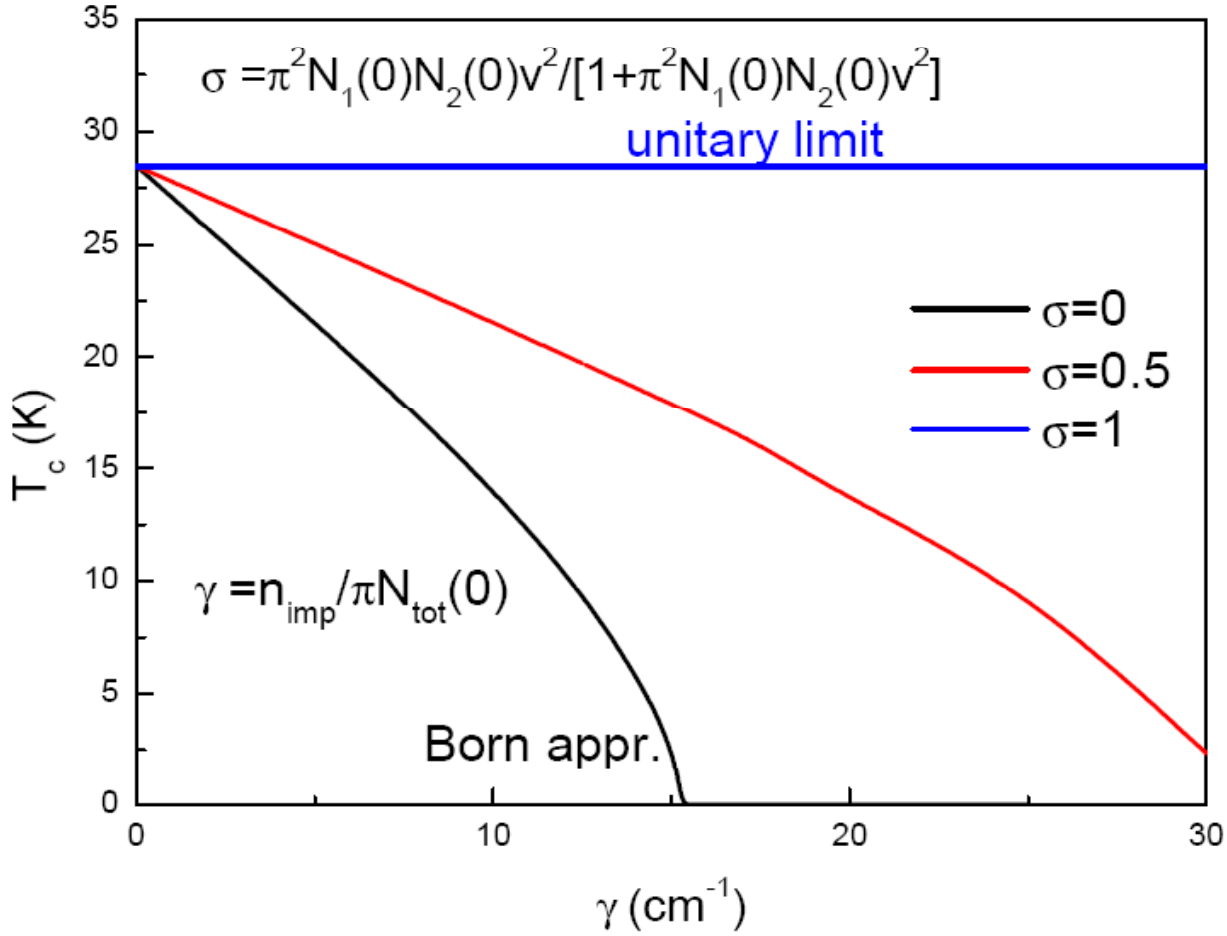
$$\det a =$$

$$\left[2\sigma(\sigma-1)\left(\sqrt{\bar{\Delta}_{an}^2 + \bar{\omega}_{an}^2}\sqrt{\bar{\Delta}_{bn}^2 + \bar{\omega}_{bn}^2} - \bar{\omega}_{an}\bar{\omega}_{bn} + \bar{\Delta}_{an}\bar{\Delta}_{bn}\right) + \sqrt{\bar{\Delta}_{an}^2 + \bar{\omega}_{an}^2}\sqrt{\bar{\Delta}_{bn}^2 + \bar{\omega}_{bn}^2}\right].$$

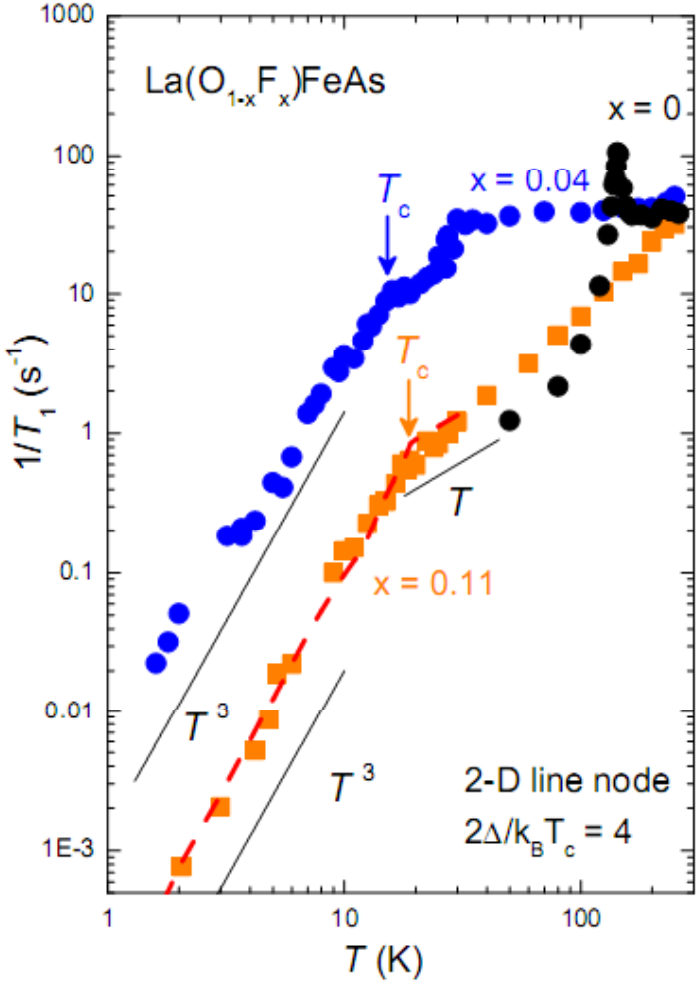
M.L.Kulić, OVD, PRB, **60**, 13062 (1999), Y. Ohashi, Physica C, **412-414**, 41(2004)

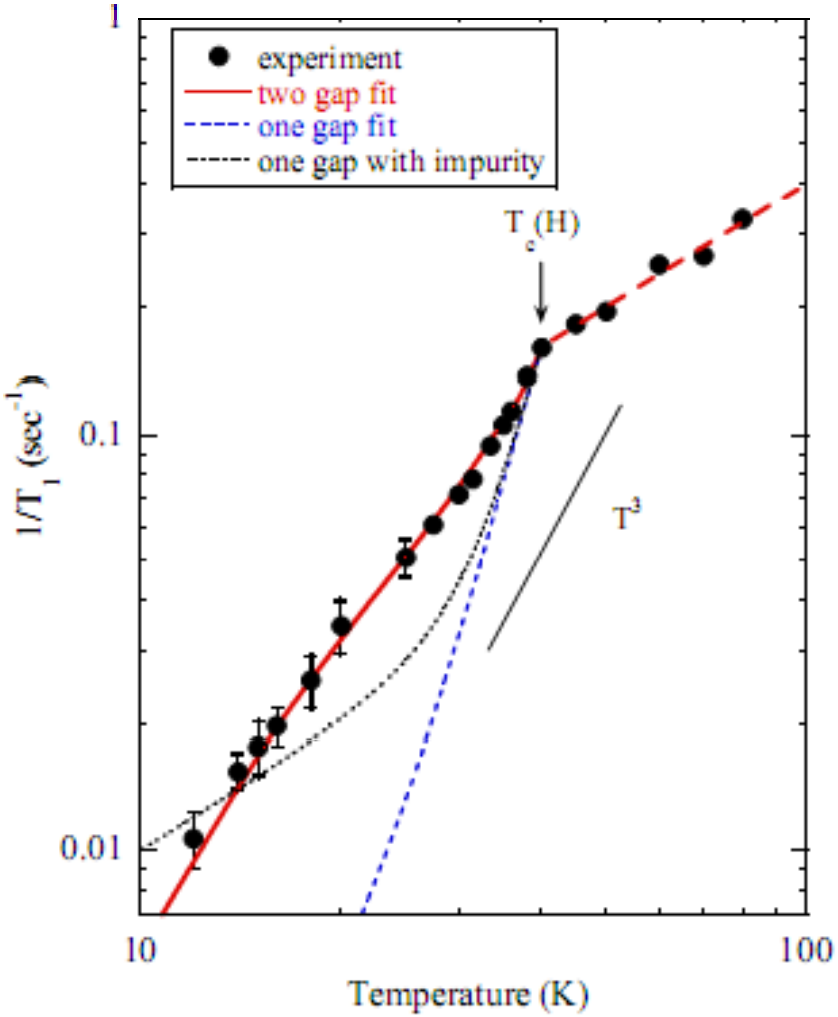
Robustness of T_c in the presence of impurities

$$\bar{\omega}_{an} = \omega_n + \gamma_{ab} sign\omega_n$$
$$\bar{\Delta}_{an} = \Delta_{an} + \gamma_{ab}\left[\sigma\bar{\Delta}_{an}/\bar{\omega}_{an} - (1-\sigma)\bar{\Delta}_{bn}/\bar{\omega}_{bn}\right] sign\omega_n$$



NMR experiments: superconductivity





^{75}As NMR: $1/T_1$ with a T^3 behavior (line of nodes?)

Y. Nakai et al., JPSJ 77, 073701 (2008)

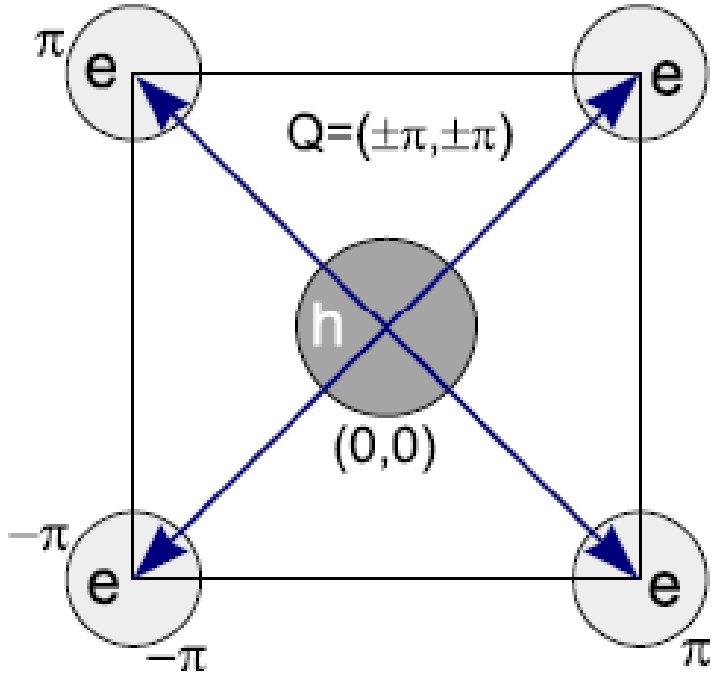
^{19}F NMR: $1/T_1$ can be explained by a two d-wave gap scenario, $\Delta = \Delta_1 + \Delta_2$, $\Delta_1 = 3.5\ k_B T_c$, $\Delta_2 = 1.1 k_B T_c$

K. Matano et al., EPL 83, 57001 (2008)

How to reconcile $s_{\pm}$ model with NMR $1/T_1$?

Use simplest model

Two types of pockets (h and e) at the Fermi surface in the *folded* BZ, reproduce LDA topology



Obtain spin-lattice relaxation rate using interband susceptibility χ_{12}:

$$1/T_1T \propto \lim_{\omega\to 0} \mathrm{Im}\, \chi_{12}(\omega)/\omega$$

Absence of the Hebel-Slichter peak

Weak coupling:

$$\frac{1}{T_1 T} \propto \sum_{\mathbf{k}\mathbf{k}'} \left(1 + \frac{\Delta_1 \Delta_2}{E_{\mathbf{k}} E_{\mathbf{k}'}}\right) \left[-\frac{\partial f(E_{\mathbf{k}})}{\partial E_{\mathbf{k}}}\right] \delta(E_{\mathbf{k}} - E_{\mathbf{k}'})$$

s-wave

$$\Delta_1 = \Delta_2 = \Delta$$

$$\boxed{\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \operatorname{sech}^2\left(\frac{E}{2T}\right)}$$

Hebel-Slichter peak

Absence of the Hebel-Slichter peak

Weak coupling: $$\frac{1}{T_1T} \propto \sum_{\mathbf{k}\mathbf{k}'} \left(1 + \frac{\Delta_1\Delta_2}{E_{\mathbf{k}}E_{\mathbf{k}'}}\right)\left[-\frac{\partial f(E_{\mathbf{k}})}{\partial E_{\mathbf{k}}}\right]\delta(E_{\mathbf{k}} - E_{\mathbf{k}'})$$

s-wave

$\Delta_1 = \Delta_2 = \Delta$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \mathrm{sech}^2\left(\frac{E}{2T}\right)$$

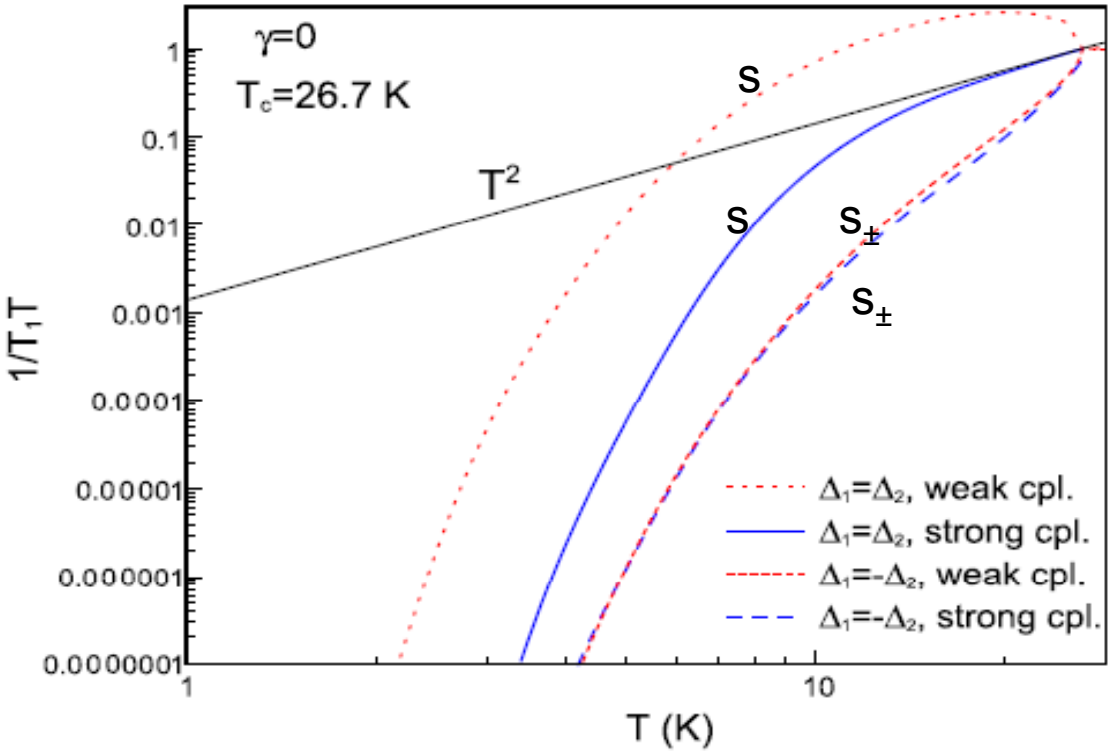
Hebel-Slichter peak

simplest $s_\pm$-wave

$\Delta_1 = -\Delta_2 = \Delta$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 - \Delta^2}{E^2 - \Delta^2} \mathrm{sech}^2\left(\frac{E}{2T}\right) = \int_{\Delta(T)}^{\infty} dE\ \mathrm{sech}^2\left(\frac{E}{2T}\right)$$

No Hebel-Slichter peak!



Strong-coupling limit

$$\frac{1}{T_1T} \propto \int_0^\infty d\omega \left(-\frac{\partial f(\omega)}{\partial \omega}\right)\{[\mathrm{Re}g_1^Z(\omega)+\mathrm{Re}g_2^Z(\omega)]^2 + [\mathrm{Re}g_1^\Delta(\omega)+\mathrm{Re}g_2^\Delta(\omega)]^2\}.$$

Here

$$g_i^Z(\omega) = n_i(\omega)Z_i(\omega)\omega/D_i(\omega)$$
$$g_i^\Delta(\omega) = n_i(\omega)\phi_i(\omega)/D_i(\omega)$$
$$D_i(\omega)=\sqrt{[Z_i(\omega)\omega]^2-\phi_i^2(\omega)}$$
$$\phi_i(\omega)=Z_i(\omega)\Delta_i(\omega)$$

$Z_i(\omega)$ is the mass renormalization
$n_i(\omega)$ is a partial density of states

complex order parameter

EEliashberg equations:

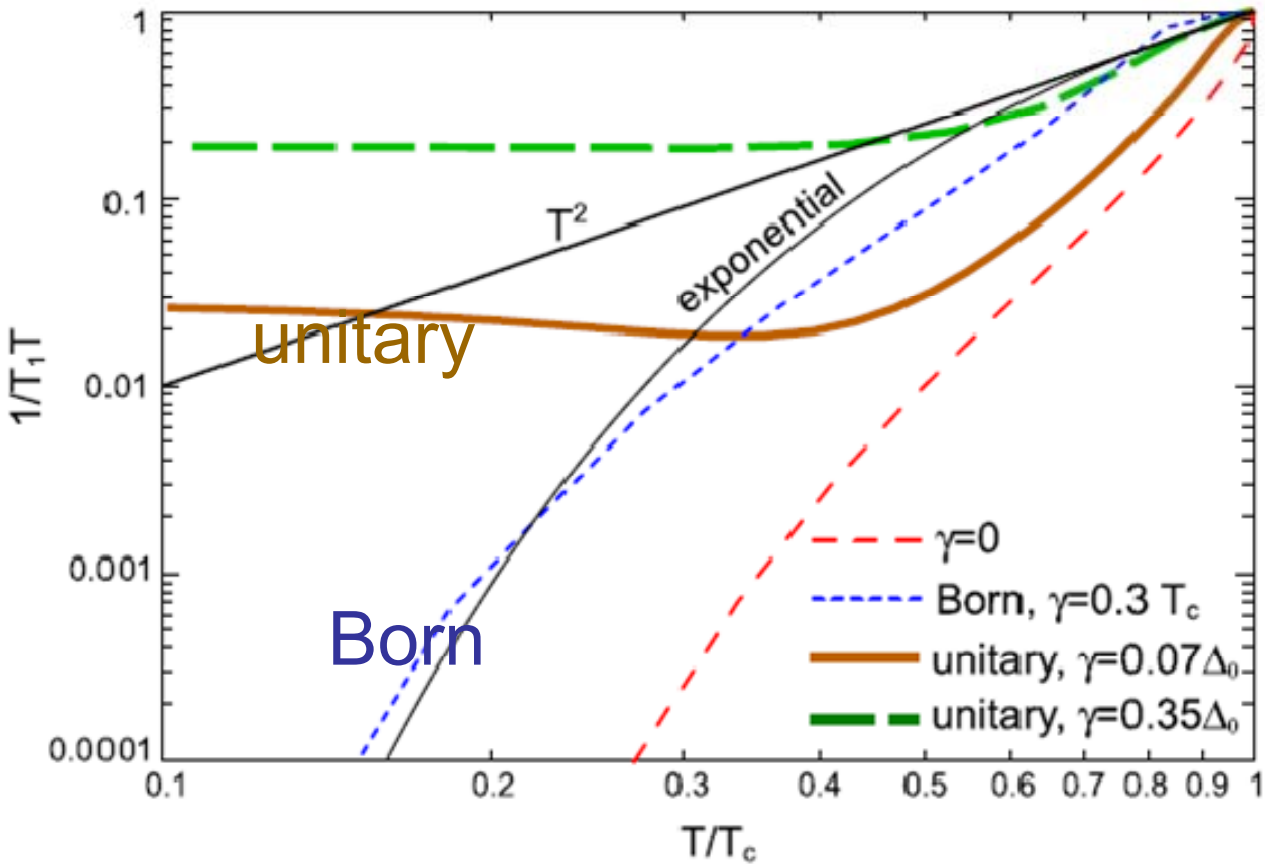
$$\phi_i(\omega) = \sum_j \int_{-\infty}^{\infty} dz K_{ij}^\Delta(z,\omega)\mathrm{Re}g_j^\Delta(z) + i\gamma\frac{g_1^\Delta(\omega)-g_2^\Delta(\omega)}{2\mathcal{D}}$$
$$(Z_i(\omega)-1)\omega = \sum_j \int_{-\infty}^{\infty} dz K_{ij}^Z(z,\omega)\mathrm{Re}g_j^Z(z) + i\gamma\frac{g_1^Z(\omega)+g_2^Z(\omega)}{2\mathcal{D}}$$

$$\sigma=\frac{[\pi N(0)v]^2}{1+[\pi N(0)v]^2}$$

$$\mathcal{D}=1-\sigma+\sigma\{[g_1^Z(\omega)+g_2^Z(\omega)]^2-[g_1^\Delta(\omega)-g_2^\Delta(\omega)]^2\}$$

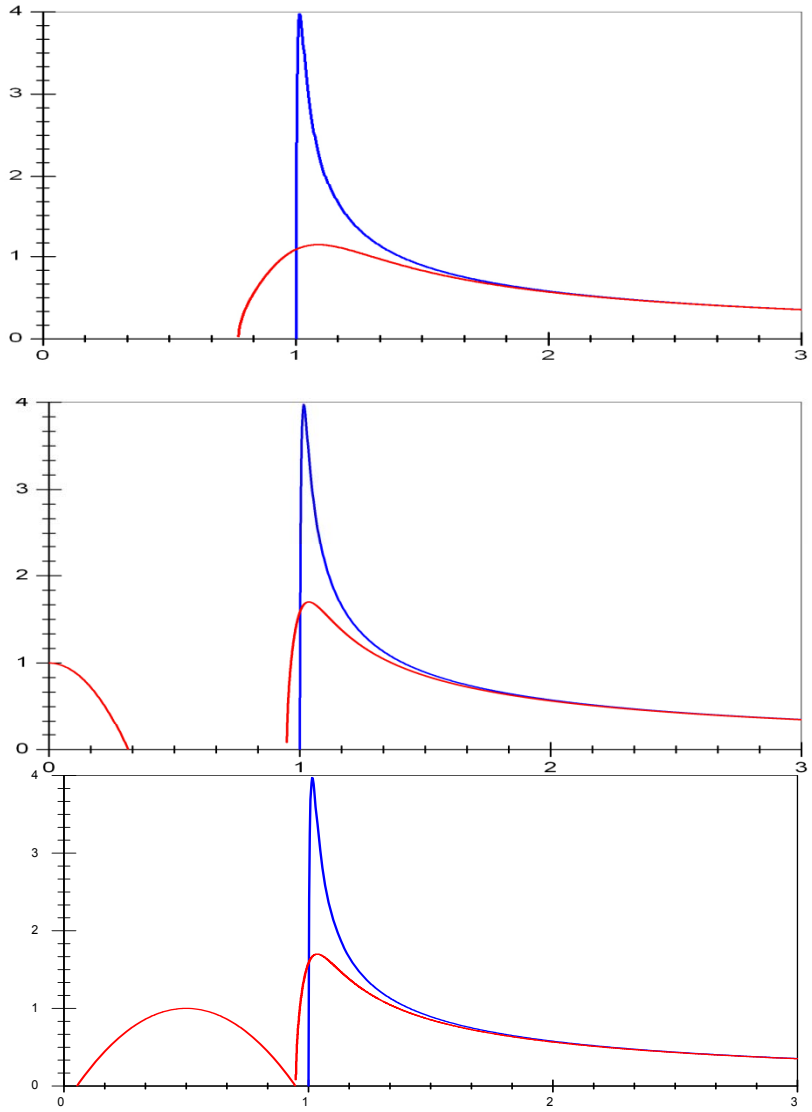
$\gamma=2c\sigma/N(0)$ is the normal-state scattering rate,
c is the impurity concentration, v is the impurity potential, σ is the impurity strength ($\sigma\rightarrow 0$: Born limit, $\sigma=1$: unitary limit)

The dependence of 1/T1 is not reproduced in both Born and unitary limits:

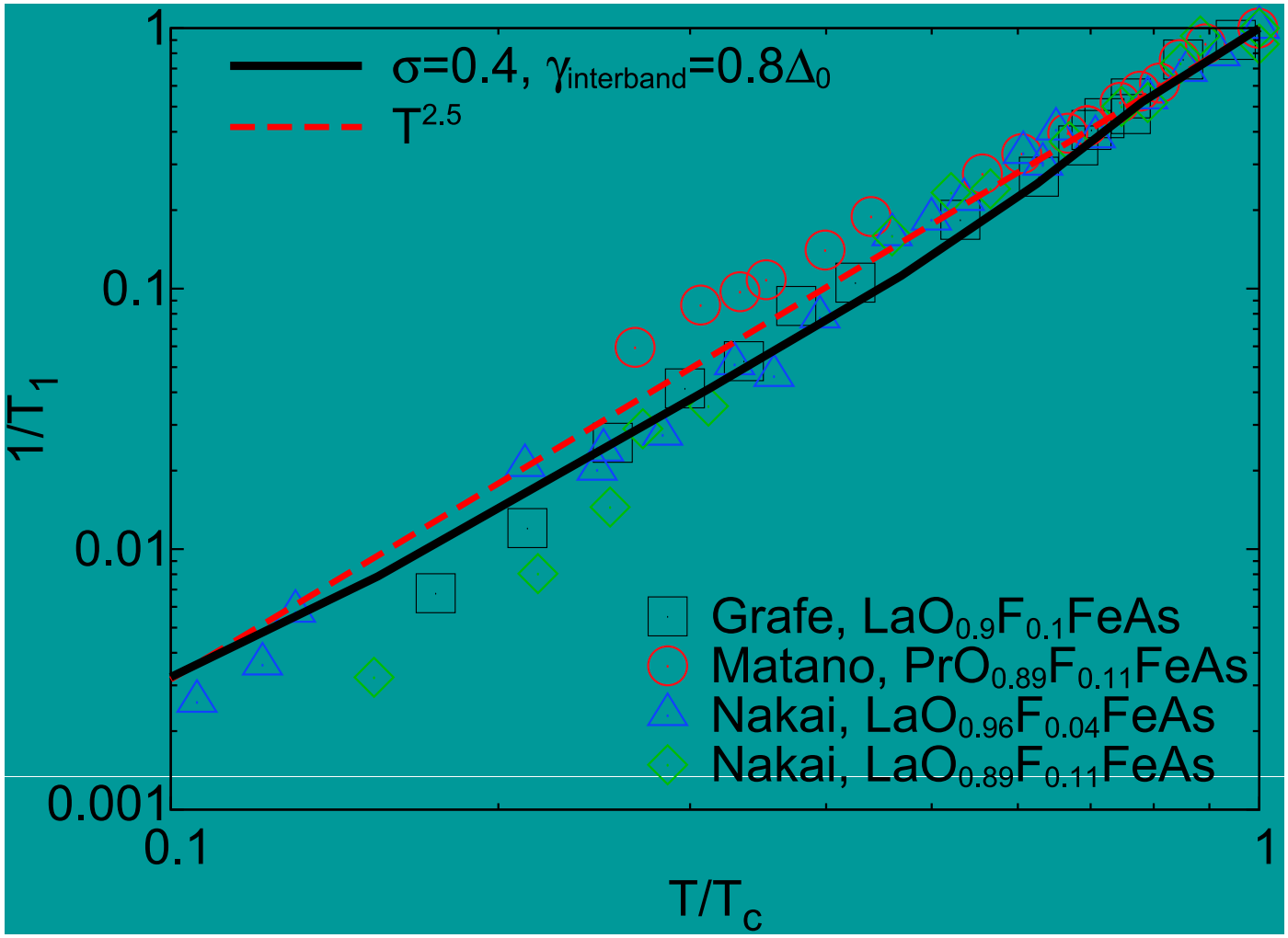


Impurity scattering: intermediate regime

1. Nonmagnetic impurities are pair breaking
2. Born limit: no coherence peak, exponential at low T
3. Unitary limit: weak Tc suppression, zero-energy bound state
4. Intermediate limit: finite energy bound state, simulates power law

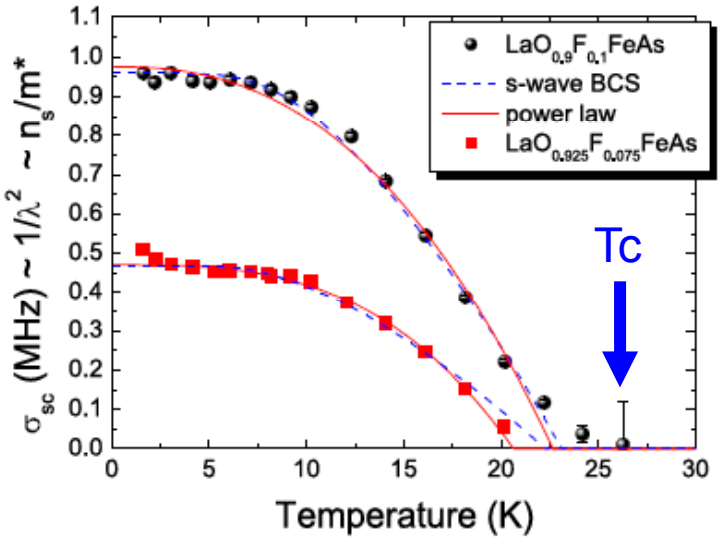


NMR: possible explanation of low-T behavior

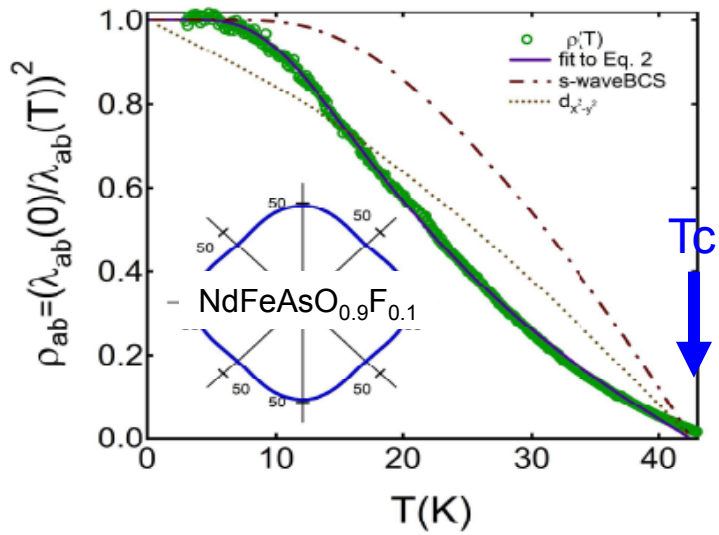


Superfluid density n_s : experiment

μSR: Luetkens, arXiv:0804.3115



μSR: Martin et al, arXiv:0807.0876



Superfuid density: the model

$$1/\lambda^2_{L,\alpha\beta}(T) \equiv (\omega^{sf}_{p,\alpha\beta}(T)/c)^2 =$$

$$\sum_{i=\sigma,\pi}\left(\frac{\omega^{\alpha\beta}_{p,i}}{c}\right)^2 \pi T \sum_{n=-\infty}^{\infty} \frac{\tilde{\Delta}^2_i(n)}{[\tilde{\omega}^2_i(n)+\tilde{\Delta}^2_i(n)]^{3/2}}$$

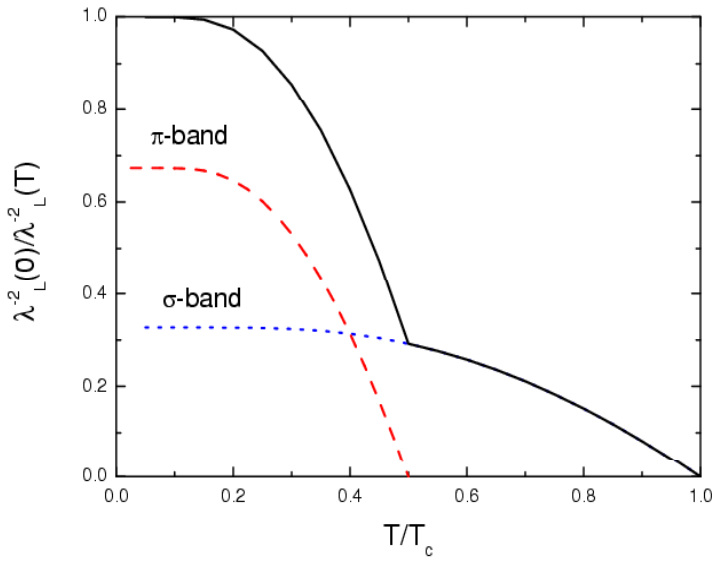
where $\tilde{\omega}(n) = \omega_n Z(\omega_n)$ and $\tilde{\Delta}(\omega_n) = \Delta(\omega_n)Z(\omega_n)$ are the solutions of the Eliashberg equations.

The case of weakly coupled bands (MgB2)

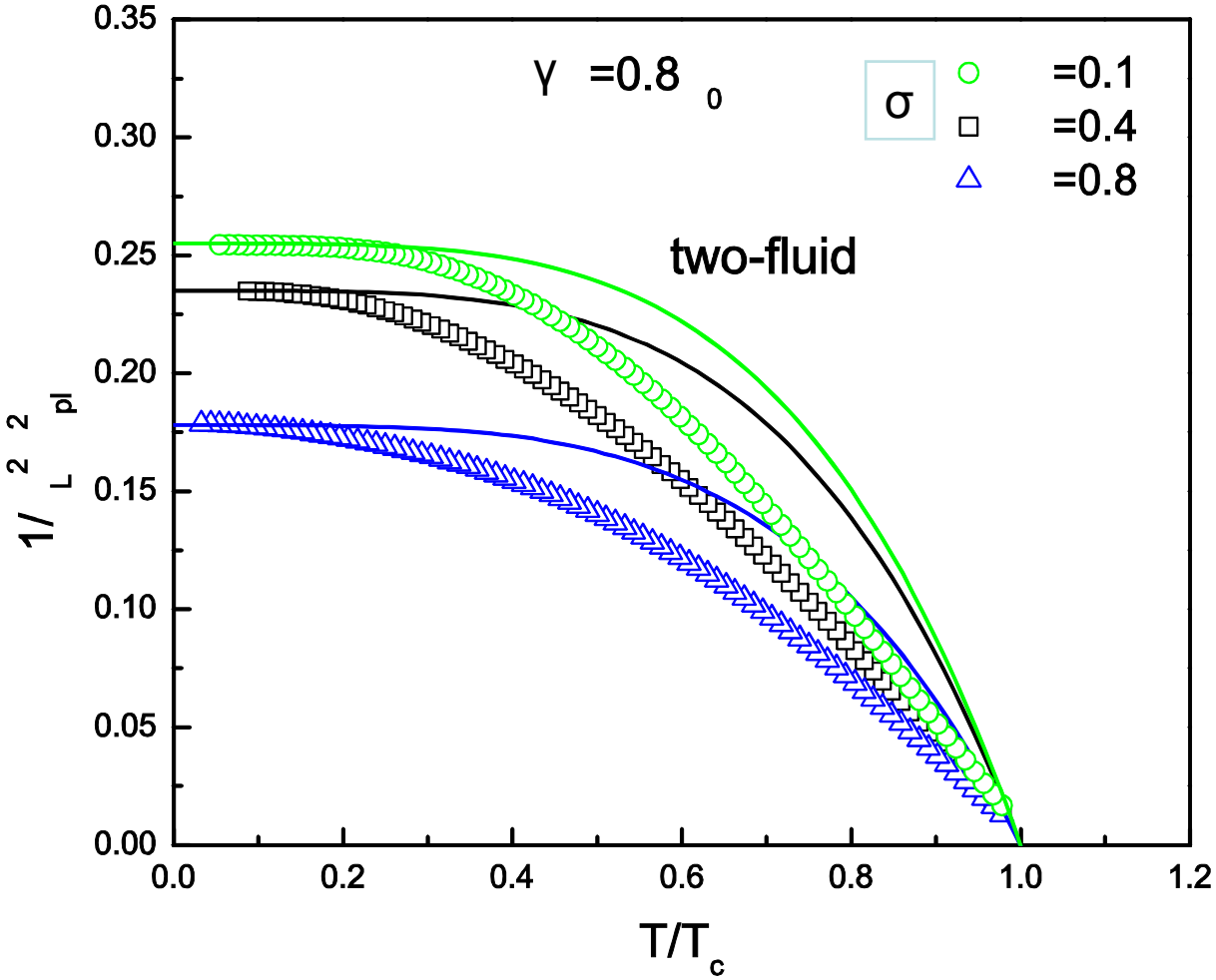
Effects of impurities

$$\Delta_i \rightarrow \Delta^0_i + \sum_j \gamma_{ij}\Delta_j/2\sqrt{\omega^2_n+\Delta^2_j}\,,$$

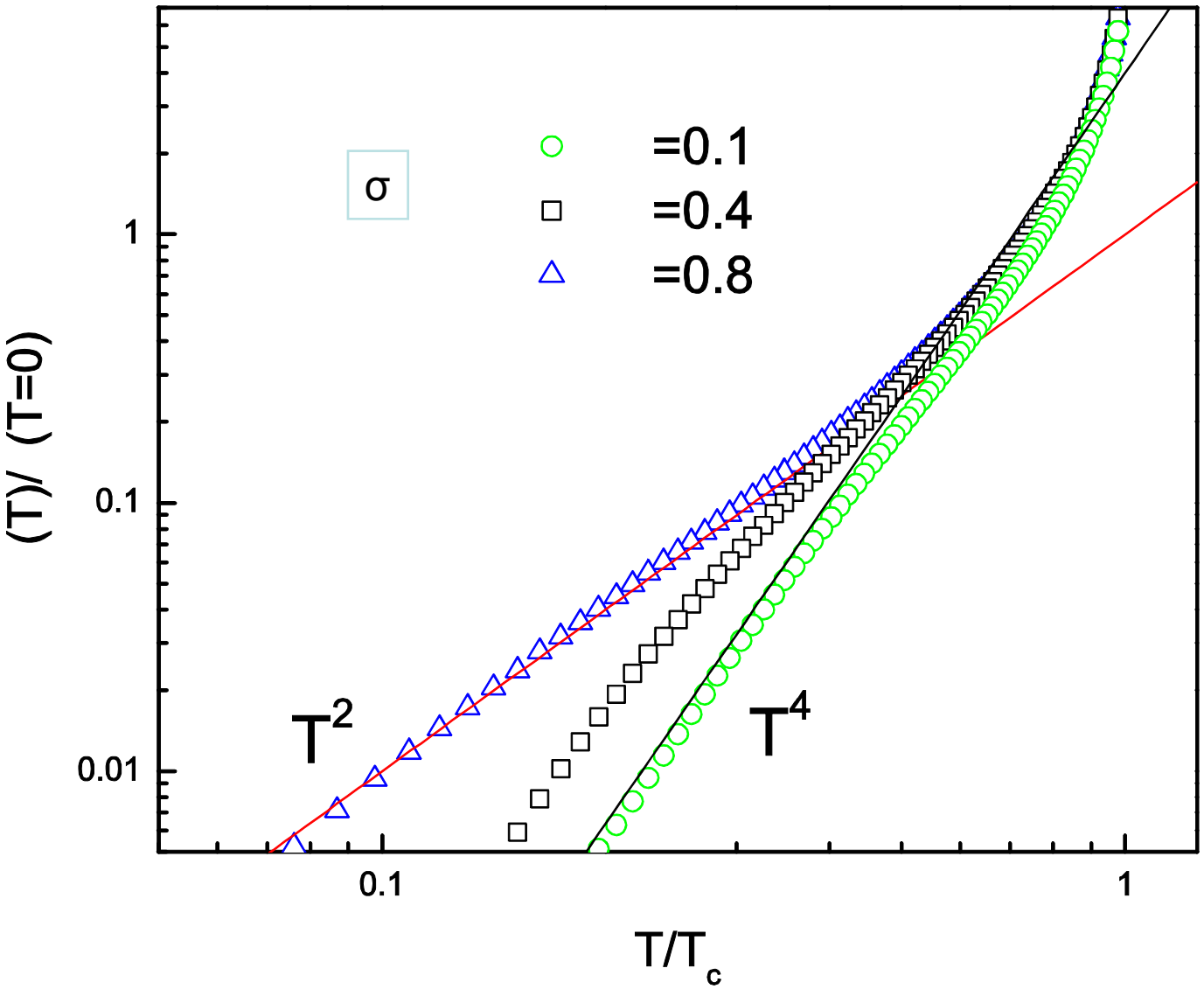
$$Z(\omega_n) \rightarrow Z^0(\omega_n) + \sum_j \gamma_{ij}/2\sqrt{\omega^2_n+\Delta^2_j}$$



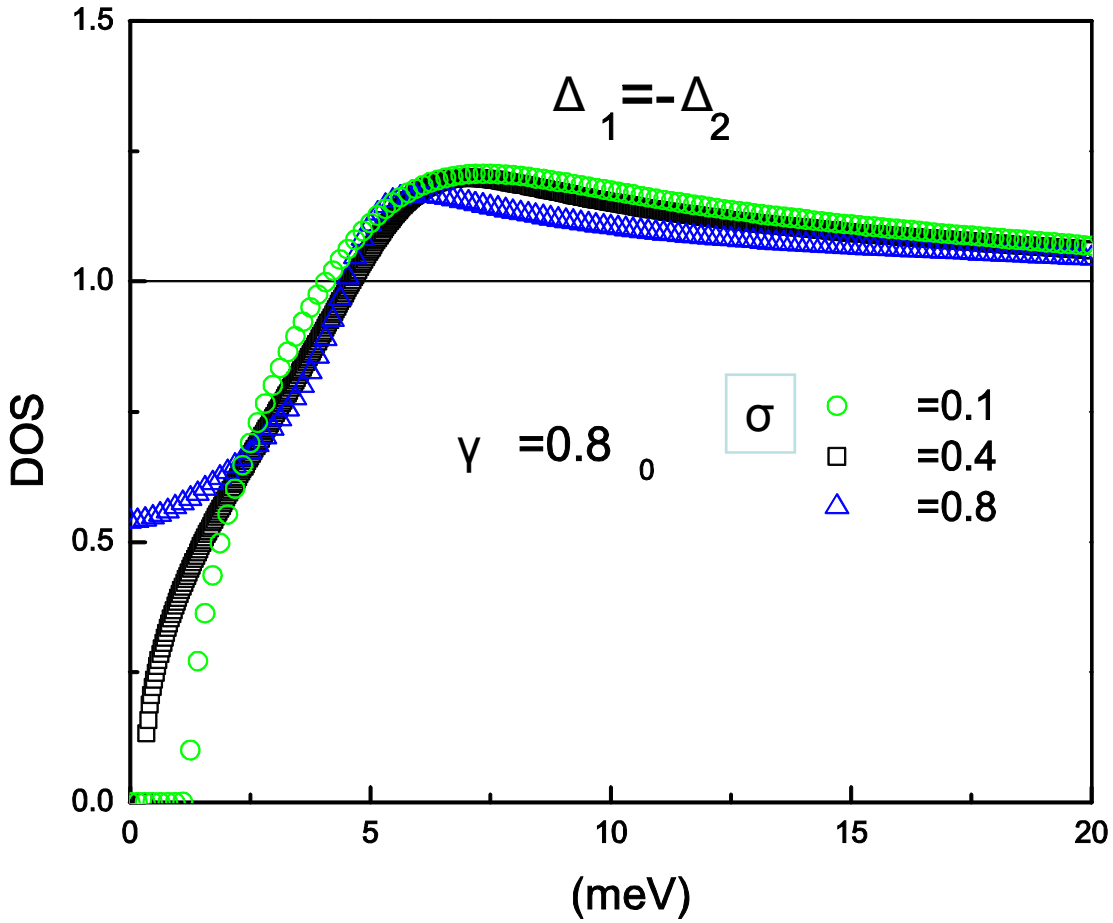
Magnetic field penetration depth



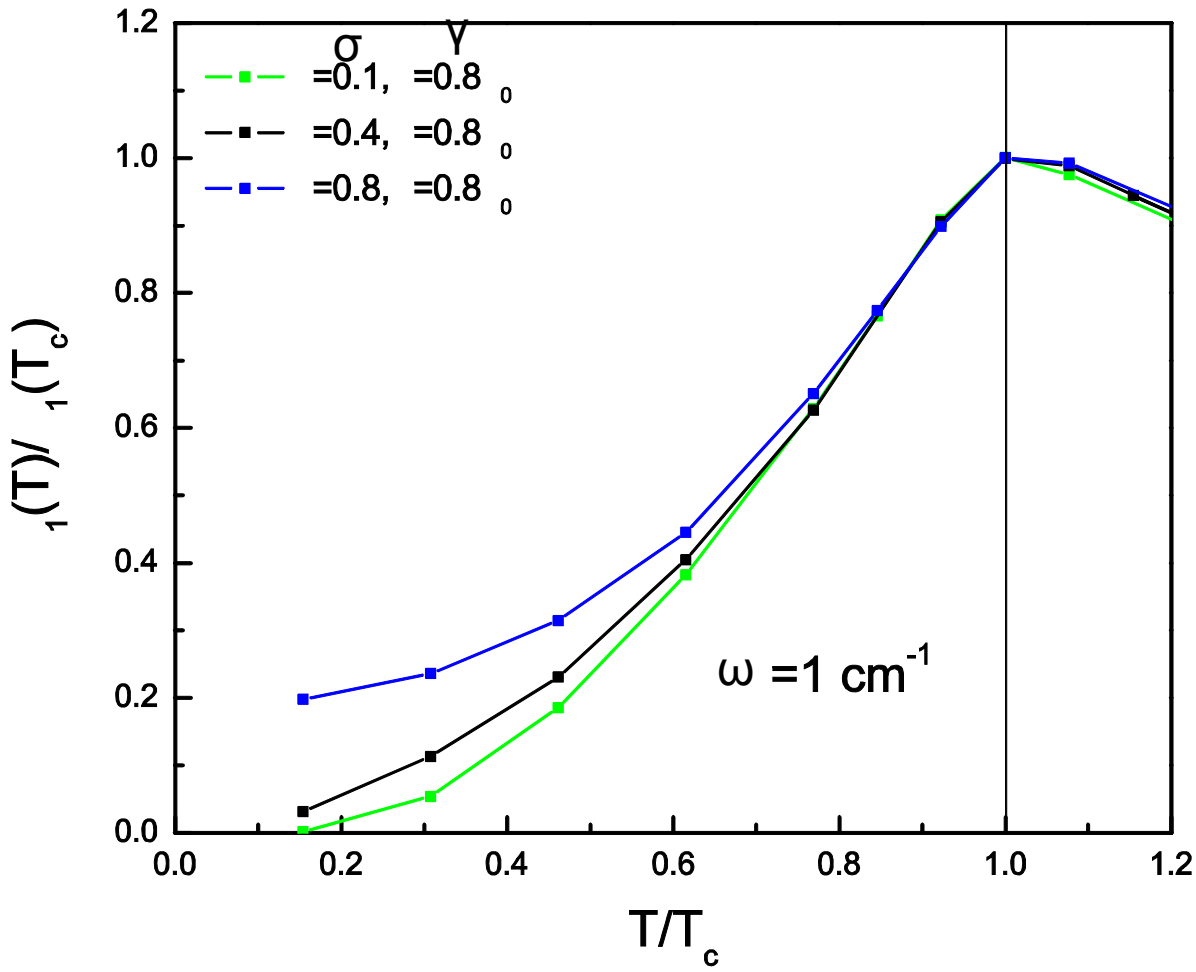
Magnetic field penetration depth: low T



Low energy density of states (DOS)



The microwave conductivity $\sigma_1(T)$



The model for tunneling in N/S junction: extending Andreev reflection formalism (the BTK model) to two bands

$$\Psi = \Psi_N \theta(-x) + \Psi_S \theta(x)$$

$$\Psi_N = \psi_k \begin{pmatrix} 1 \\ 0 \end{pmatrix} + a\psi_k \begin{pmatrix} 0 \\ 1 \end{pmatrix} + b\psi_{-k} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\Psi_S = c \left[\beta\phi_p \begin{pmatrix} u_1 \\ v_{1+} e^{-i\varphi_1} \end{pmatrix} + \alpha\phi_q \begin{pmatrix} u_2 \\ v_{2+} e^{-i\varphi_2} \end{pmatrix} \right]$$

$$+ d \left[\beta\phi_p \begin{pmatrix} v_1 \\ u_1 e^{-i\varphi_1} \end{pmatrix} + \alpha\phi_q \begin{pmatrix} v_2 \\ u_2 e^{-i\varphi_2} \end{pmatrix} \right]].$$

Φ_p are *Bloch functions*

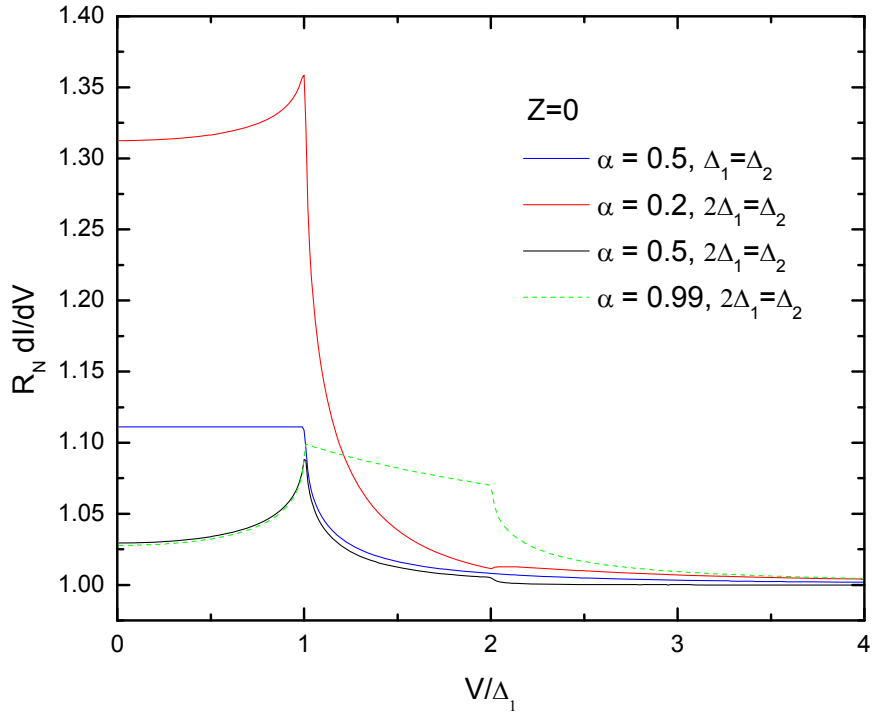
and α,β are mixing coefficients between electron and hole bands

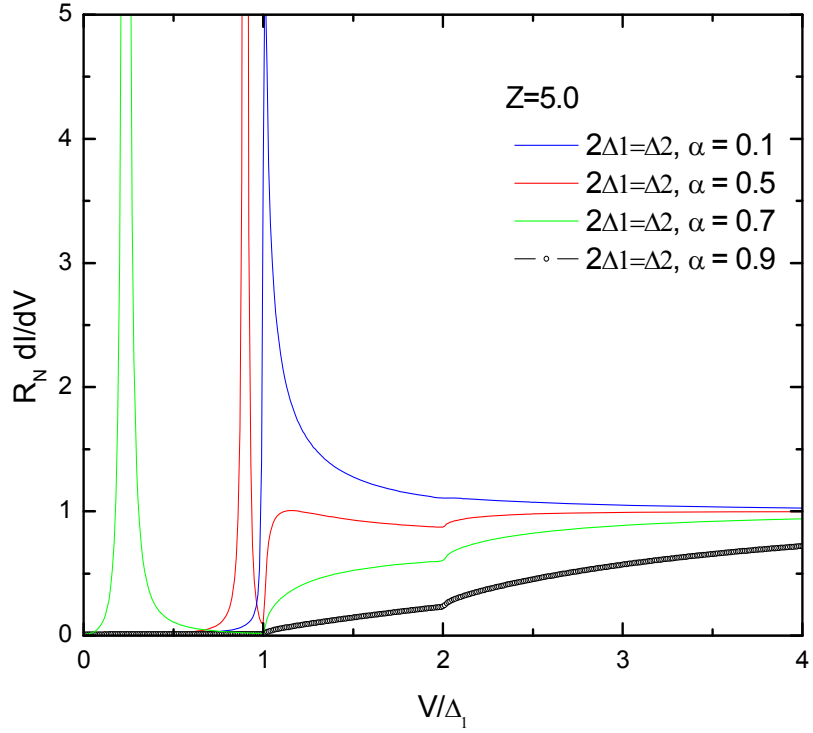
$$\alpha^2 + \beta^2 = 1$$

Tunneling conductance in the $s_{\pm}$ case

$$Z = H / \hbar v_{FN}$$

H – the barrier height

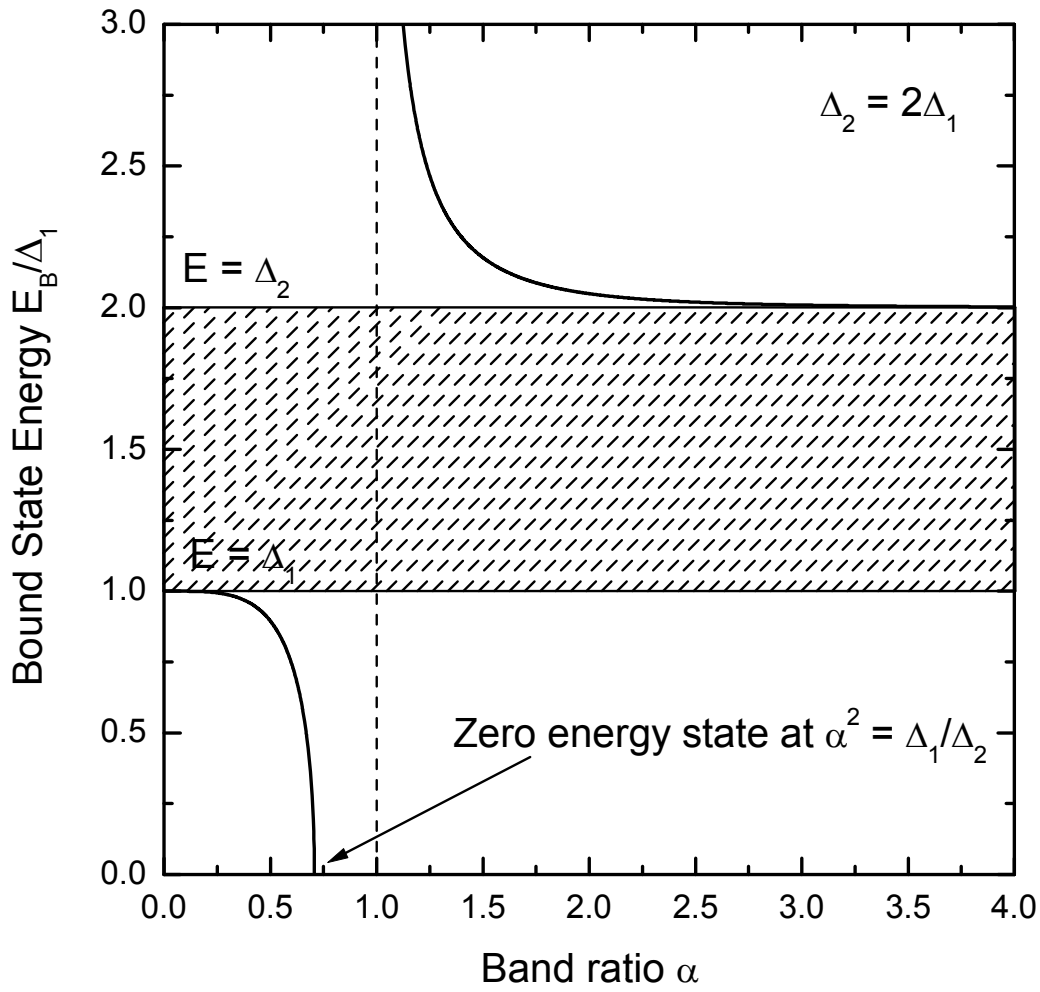




Andreev conductance is suppressed due to destructive interband interference

Bound states appear at finite energy for large Z

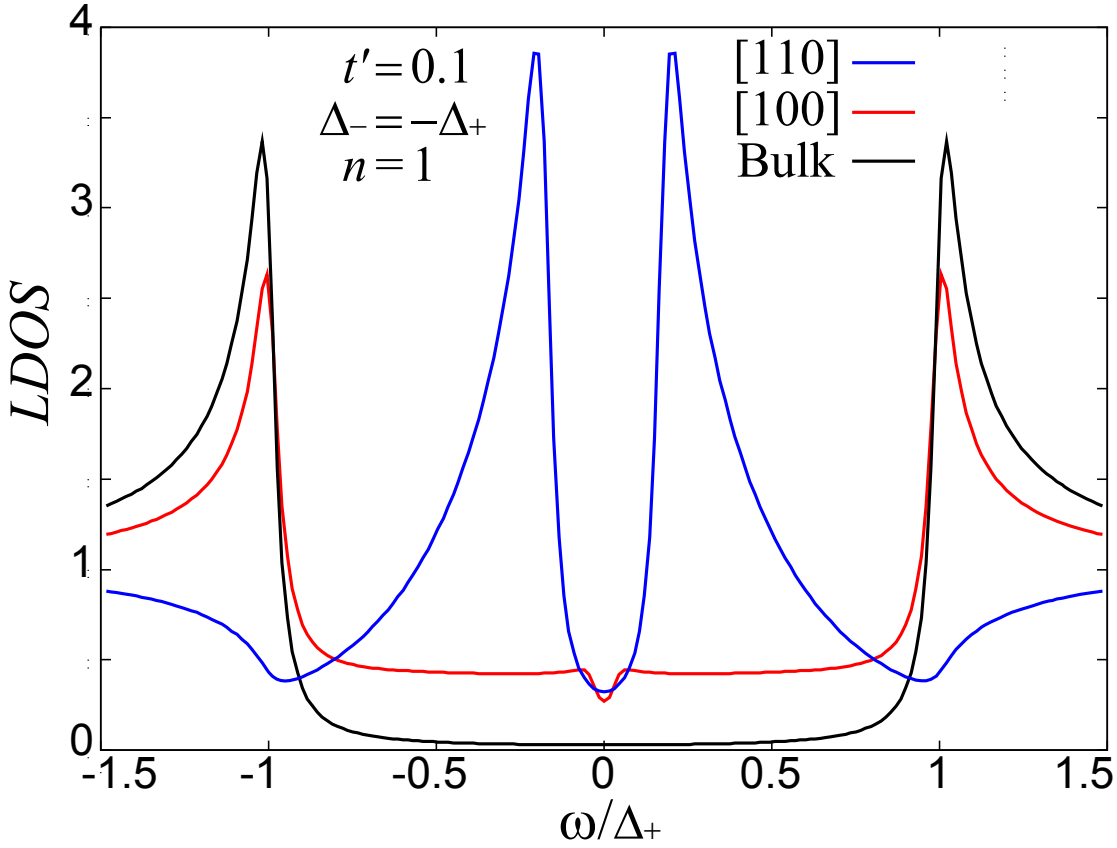
Tunneling regime: Surface bound states

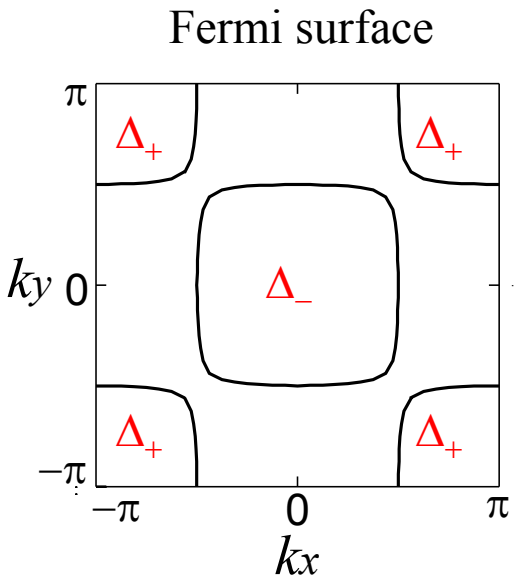


LDOS at surface

s+−wave

$\Delta_{+(-)}$=+(−)0.1





Andreev bound state with non zero energy (Onari and Tanaka)

Conclusions

- ***s*±** pairing can explain some properties of superconducting *Fe-pnictides*.

- T_c is robust against *unitary* interband scattering.

- The lack of an NMR Hebel-Slichter peak is fully consistent with the nodeless ***s*±** wave symmetry of the order parameter (whether in the clean or dirty limit).

- The low-temperature power-law behavior of $1/T_1$ can be also explained in the framework of the s± model but requires the impurity scattering beyond the Born limit.

- *Conductance Peak* can appear in *Andreev* and tunneling experiments, but, unlike nodal superconductors, at finite energy.