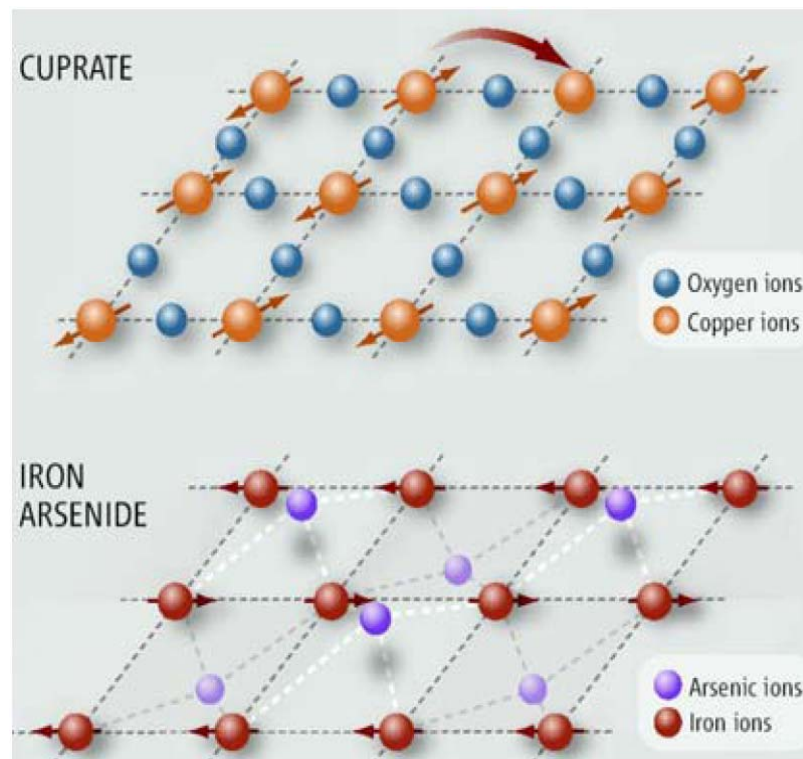


Designing phase-sensitive symmetry tests for Fe-based superconductors

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In collaboration with

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Max-Planck-Institut für Festkörperforschung,
Stuttgart

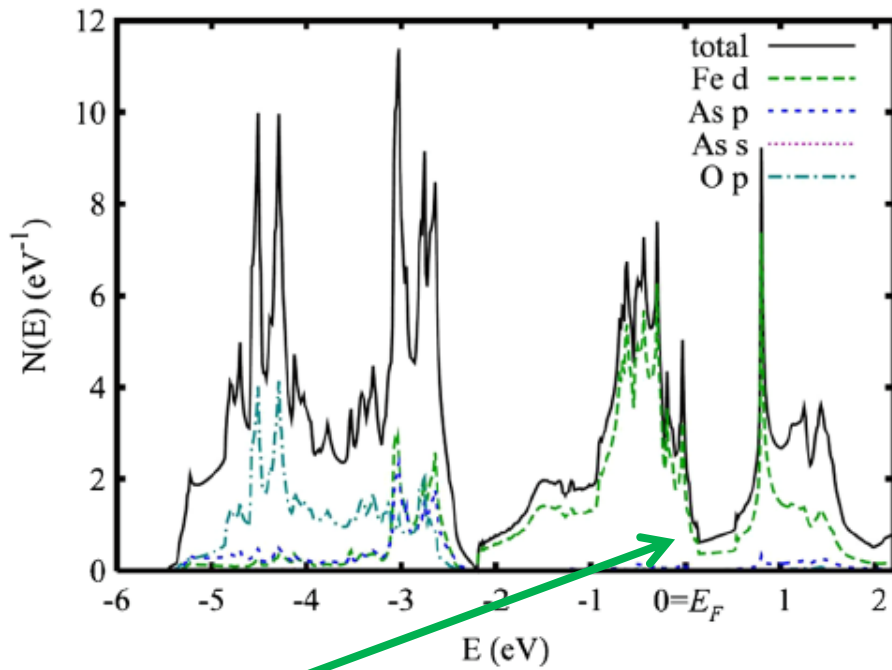
Y. Tanaka, K. Yada

Nagoya University, Japan

I.I. Mazin

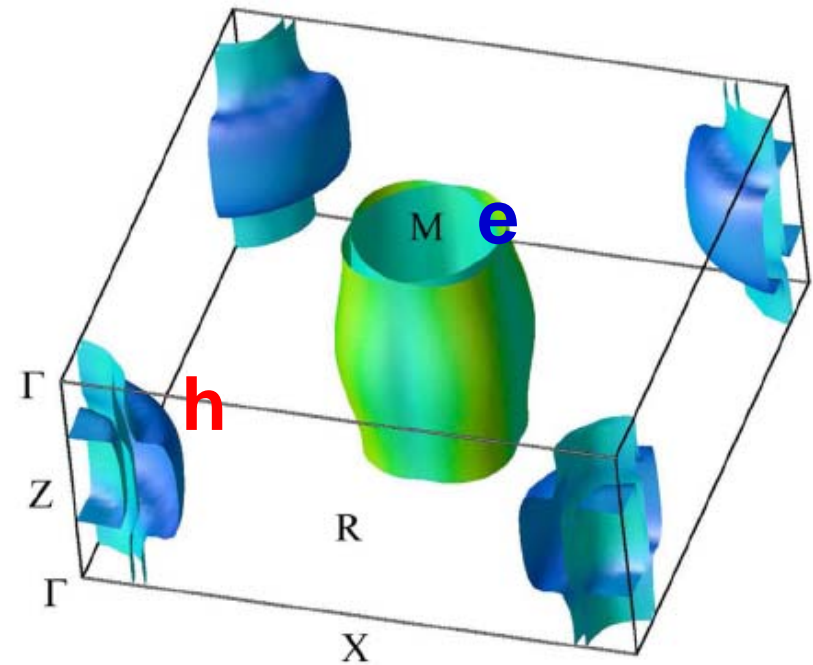
Naval Research laboratory, USA

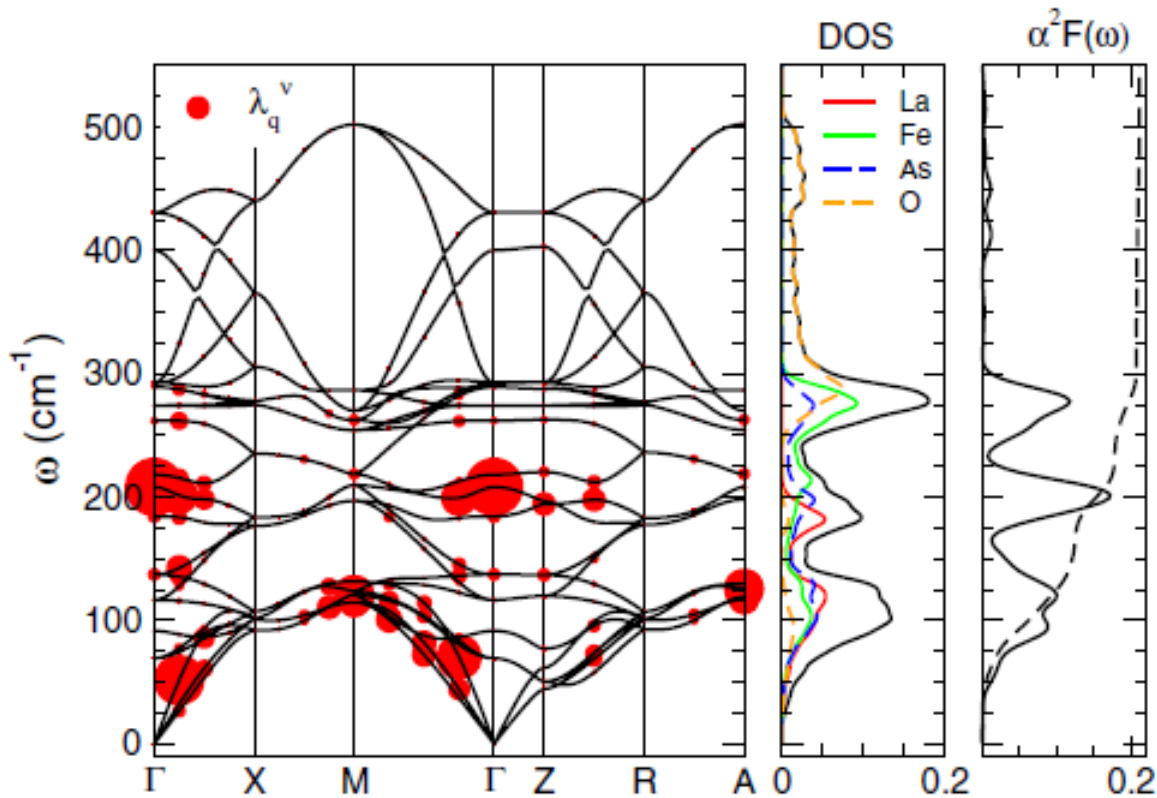
Electronic Structure



Fe²⁺ 3d⁶-states

Weak splitting: all 5 orbitals ($d_{x^2-y^2}$, d_{3z^2-1} , d_{xy} , $d_{xz}+d_{yz}$) are near of the E_F





L. Boeri, O.V. Dolgov, and A.A. Golubov, PRL 101, 026403 (2008);
 D.J. Singh and M.-H. Du, PRL 100, 237003 (2008)

↓

$$\lambda = 0.21 \quad (\text{for Al } \lambda=0.44)$$

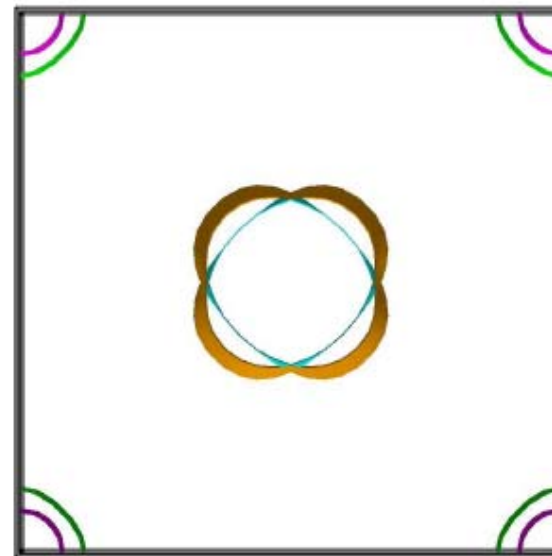
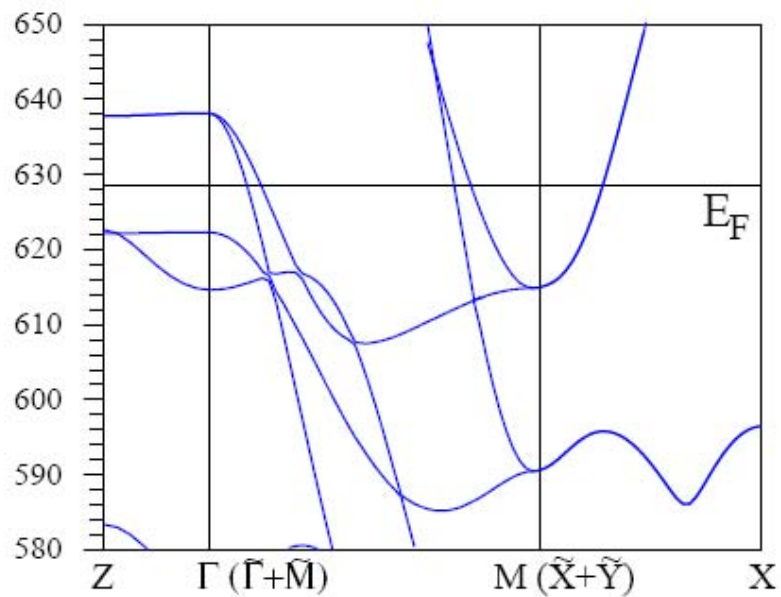
Not sufficient to explain SC!

$$\alpha^2 F(\omega) = \frac{1}{N(0)} \sum_{nm\mathbf{k}} \delta(\varepsilon_{n\mathbf{k}}) \delta(\varepsilon_{m\mathbf{k}+\mathbf{q}}) \times$$

$$\times \sum_{\nu\mathbf{q}} |g_{\nu, n\mathbf{k}, m(\mathbf{k}+\mathbf{q})}|^2 \delta(\omega - \omega_{\nu\mathbf{q}});$$

$$\lambda(\omega) = 2 \int_0^\omega d\Omega \alpha^2 F(\Omega) / \Omega$$

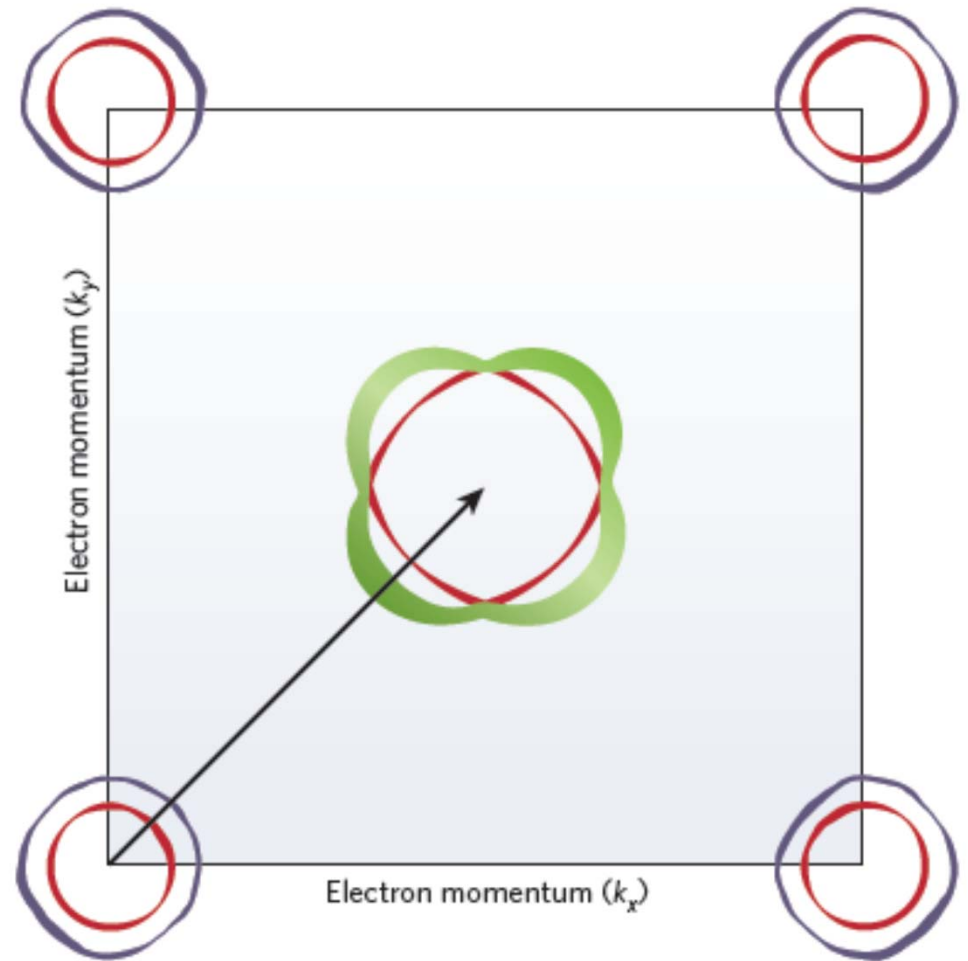
Band structure (hole doped)



Spin fluctuations

$$\chi(\mathbf{q}, \omega) = \frac{\chi_0(\mathbf{q}, \omega)}{1 - J(\mathbf{q}, \omega) \chi_0(\mathbf{q}, \omega)}$$

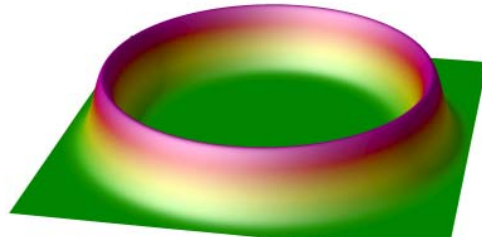
Berk-Schrieffer theory (1970's) :
 $J(\mathbf{q}, \omega)$ -magnetic interaction



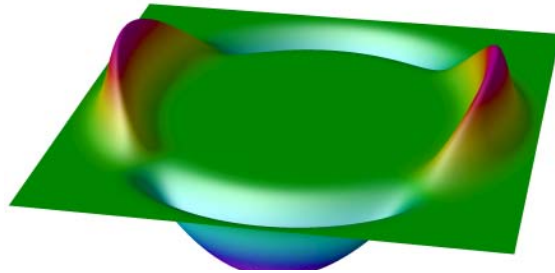
A typical Fermi surface of an iron-pnictide superconductor, projected onto the k_x - k_y plane

Various symmetries of the superconducting order parameter

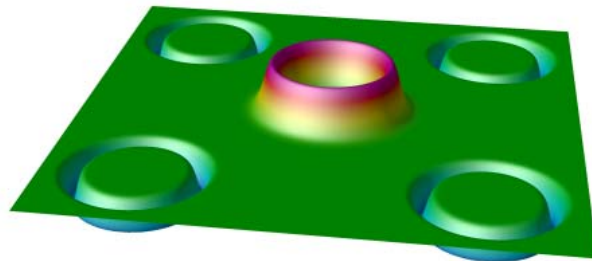
(a) a conventional S-wave



(b) a d-wave, as in cuprates

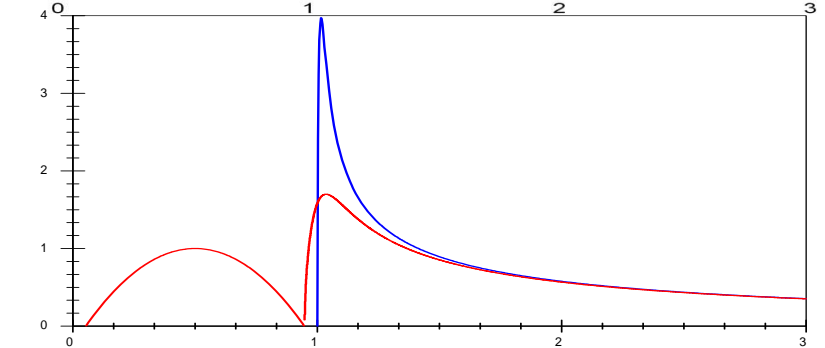
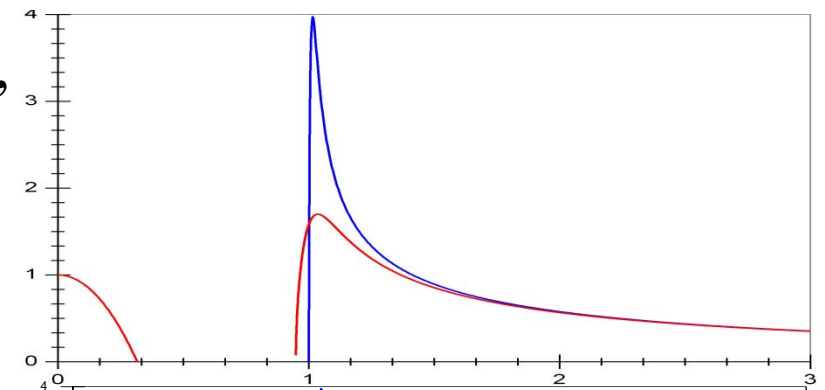
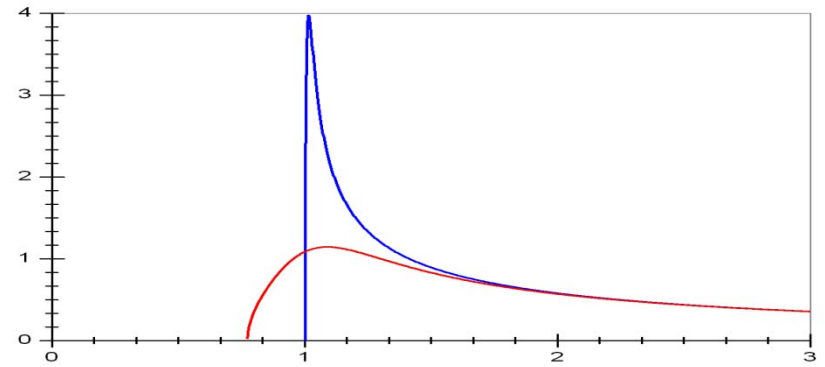


(c) s_{\pm} wave (pnictides ?)



Impurity scattering in the $s_{+/-}$ state

1. Nonmagnetic impurities are pair breaking
2. Born limit: no coherence peak, exponential at low T
3. Unitary limit: weak T_c suppression, zero-energy bound state
4. Intermediate limit: finite energy bound state, simulates power law



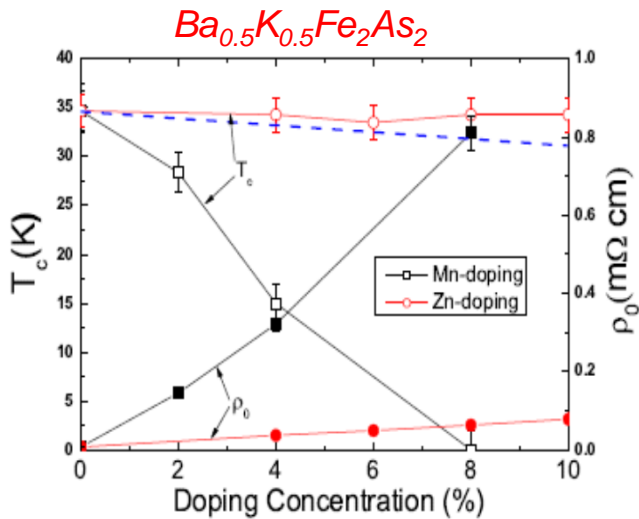
Disorder induced transition between s_{+-} and s_{++} states in two-band superconductors

D.V. Efremov, M.M. Korshunov, O.V. Dolgov, A.A. Golubov, and P.J. Hirschfeld, 'Disorder-induced transition between s_{\pm} and s_{++} states in two-band superconductors', Phys. Rev. B **84**, 180512 (2011).

D.V. Efremov, A.A. Golubov, and O.V. Dolgov, 'Manifestations of impurity induced $s_{\pm} \Rightarrow s_{++}$ transition: multiband model for dynamical response functions', New J. Phys. **15**, 013002 (2013).

- Experiments in favor **S₊₋**
 - NMR
 - Absence of Hebel-Schlichter peak
 - $1/T_1 \sim T^3 - T^5$
 - Resonance peak in neutron scattering experiments
- Experiments in favor **S₊₊**
 - Absence or weak *suppression* of T_c by *nonmagnetic* impurities.

Nonmagnetic impurities vs magnetic.

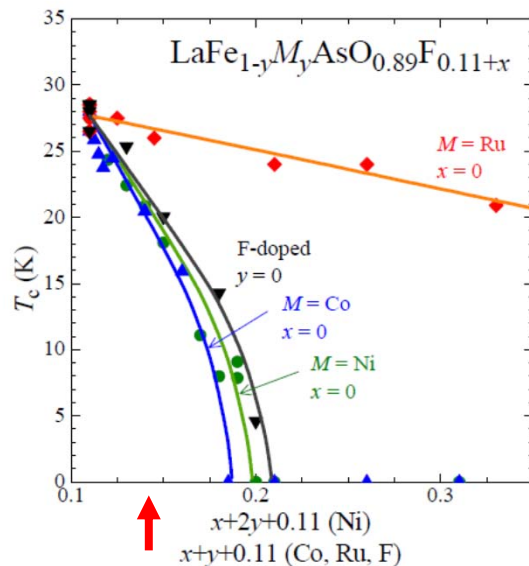


• **Common wisdom:** The impurity in S_{\pm} superconductors *suppress* T_c in the same way as paramagnetic impurity in common superconductors. T_c is given by Abrikosov-Gorkov formula:

$$\ln\left(\frac{T_{c0}}{T_c}\right) = \Psi\left(\frac{1}{2} + \frac{\Gamma_s}{2T_c}\right) - \Psi\left(\frac{1}{2}\right)$$

The critical value ($T_c(\Gamma_{crit}) = 0$) of the scattering rate is given:

$$\Gamma_{cr} / T_{c0} \approx 1.12$$



x_{crit}

Onari, Kontani, PRL**103**, 17701(2009)

- Can T_c in $s+_-$ superconductors be *robust* against interband scattering?
- If yes, what is the physical reason?

T_c : nonmagnetic impurities, weak coupling limit.

$$\lim_{T \rightarrow T_c} \tilde{\omega}_{na} = \omega_{na} + \cancel{(\gamma_{aa} + \gamma_{ab})} \text{sign}(\omega_n)$$

$$\lim_{T \rightarrow T_c} \tilde{\Delta}_{na} = \Delta_{na} + \left(\cancel{\gamma_{aa}} \frac{\tilde{\Delta}_{na}}{|\tilde{\omega}_{na}|} + \gamma_{ab} \frac{\tilde{\Delta}_{nb}}{|\tilde{\omega}_{nb}|} \right)$$

$$\gamma_{aa} = \frac{1}{2} n \pi N_a \langle |u|^2 \rangle_{FS} \quad \gamma_{ab} = \frac{1}{2} n \pi N_b \langle |v|^2 \rangle_{FS}$$

$$\langle \lambda \rangle_{FS} = \frac{1}{N_a + N_b} [N_a (\lambda_{aa} + \lambda_{ab}) + N_b (\lambda_{ba} + \lambda_{bb})]$$

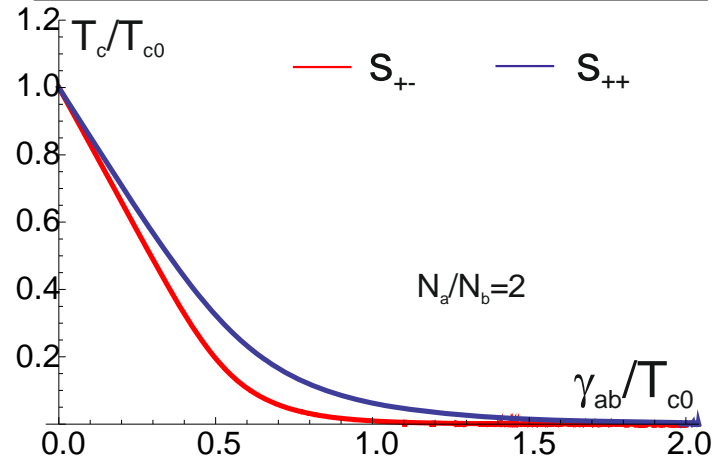
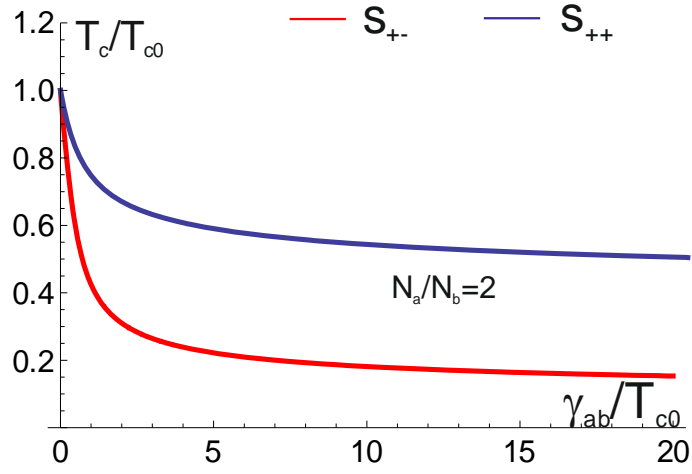
$$\langle \lambda \rangle_{FS} > 0$$

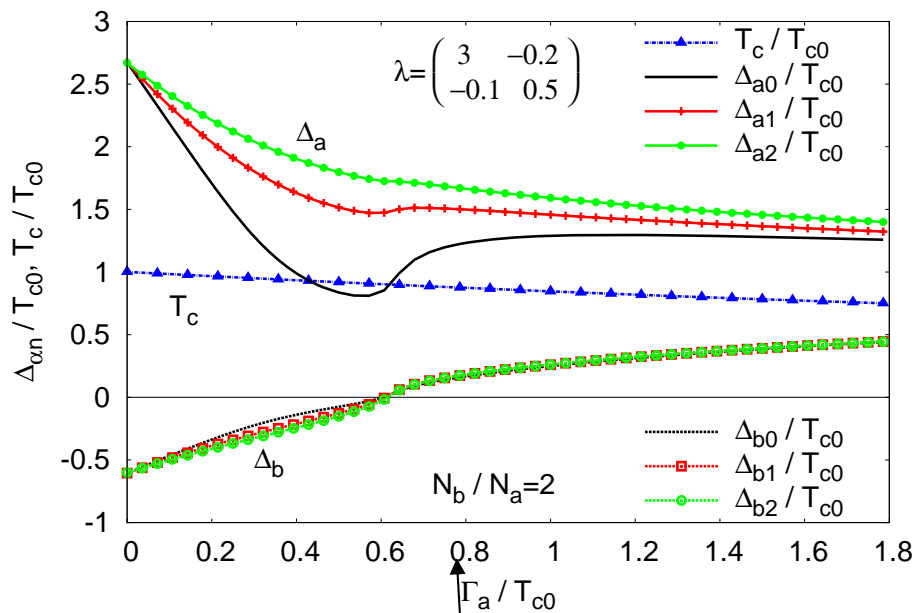
$$\langle \lambda \rangle_{FS} < 0$$

saturation to the finite value

$$T_{c\infty}^{BCS} \propto We \frac{1}{\langle \lambda \rangle_{FS}}$$

critical impurity scattering

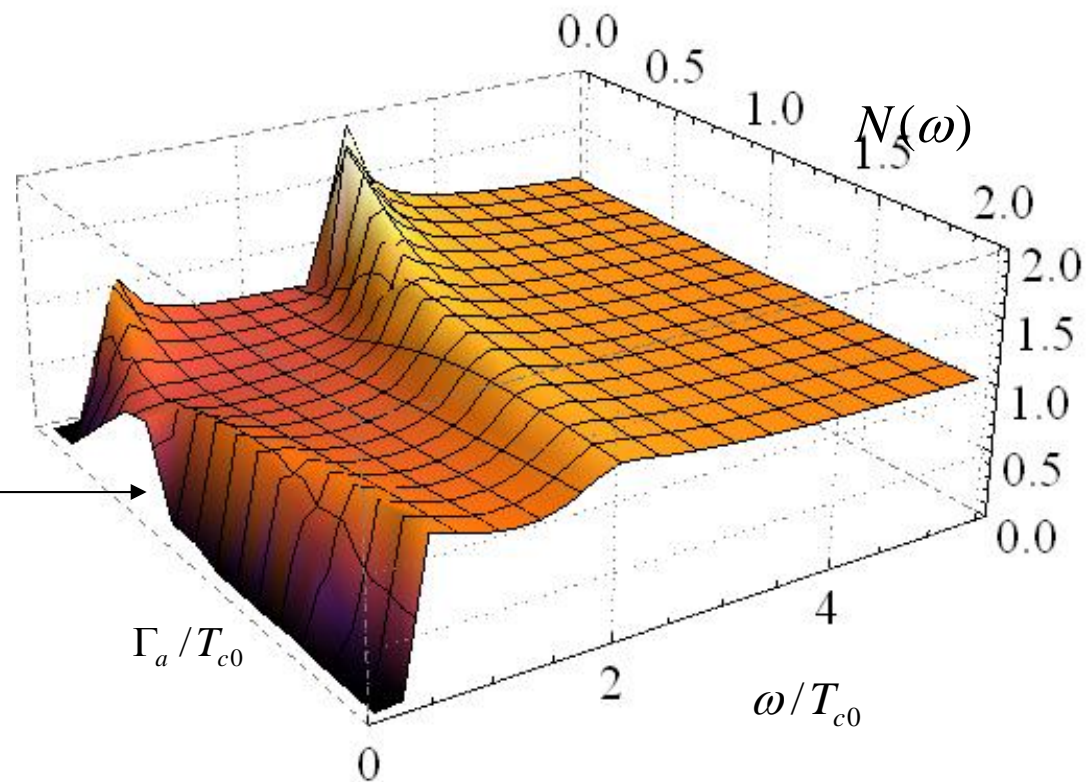
$$\gamma_{crit}^{BCS} \propto We \frac{\langle \lambda \rangle_{FS}}{\lambda_{aa}\lambda_{bb} - \lambda_{ab}\lambda_{ba}}$$




$$\Lambda = \begin{pmatrix} 3 & -0.2 \\ -0.1 & 0.5 \end{pmatrix}$$

Density of States

gapless regime



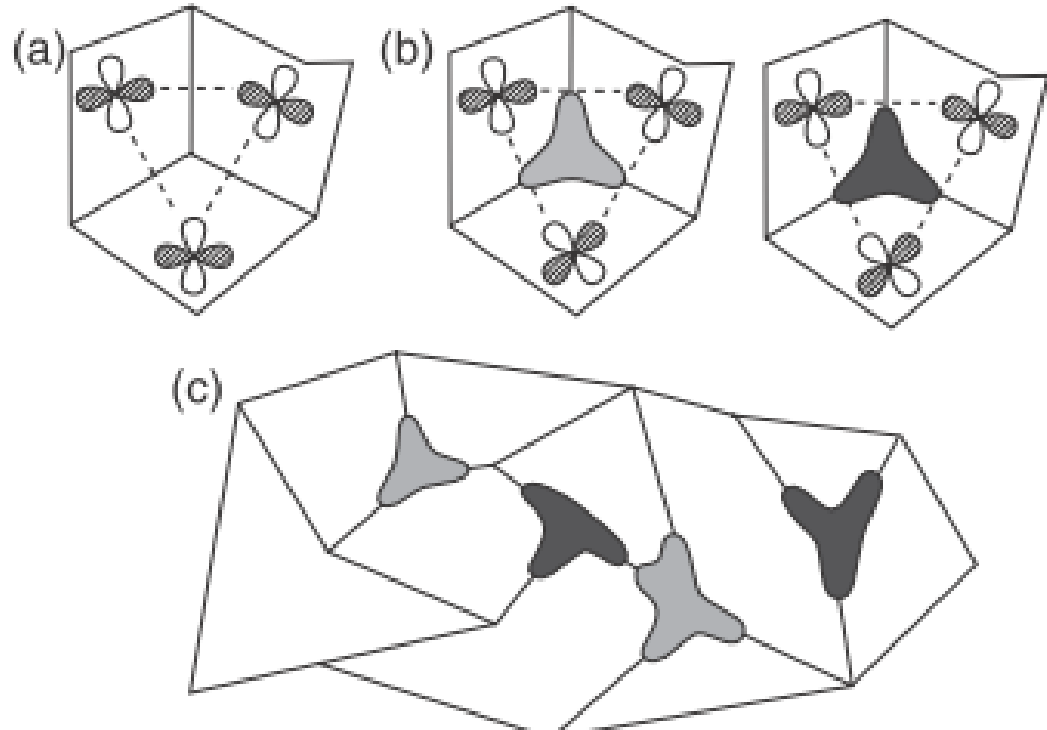
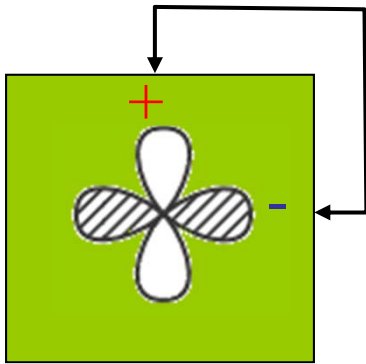
Designing phase-sensitive symmetry tests for Fe-based superconductors:

s_{+-} and s_{++} states in two-band superconductors

Josephson effects in pnictide junctions

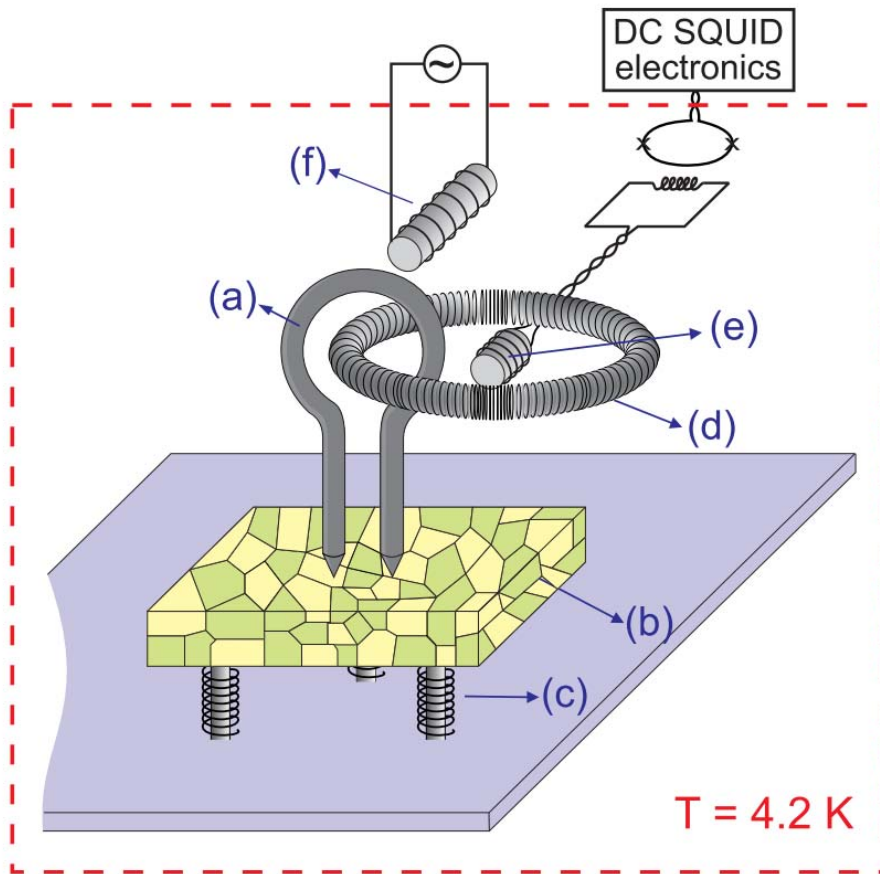
- c-axis Josephson: *observed (UMD group)*
- Paramagnetic Meissner (Wohleben) effect; *not observed (K.A. Moler et al, JPSJ)*

D-wave symmetry:
corner junctions and
tricrystal rings



Sign change of the order parameter

IBM group (Tsuei et al), Nature, 2010



Half-integer fluxes detected (in a small fraction of loops).

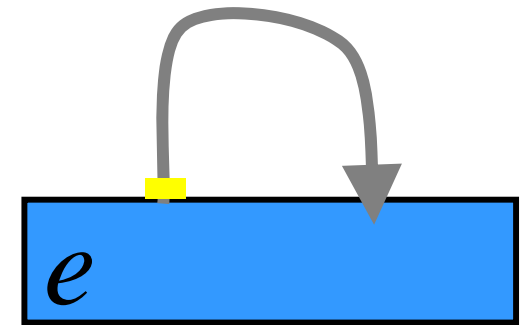
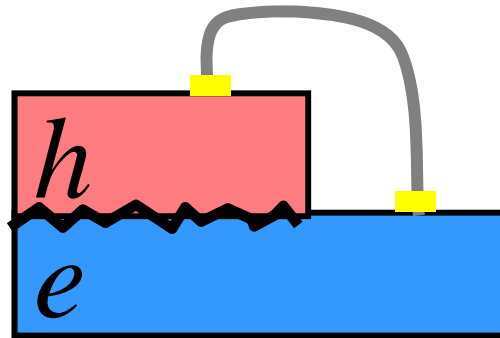
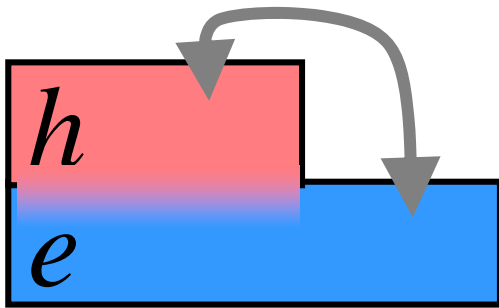
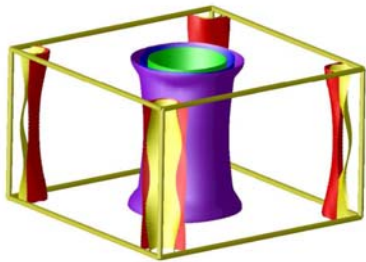
Various interpretations possible, but all of them require sign change of the order parameter

-> indicates sign changes

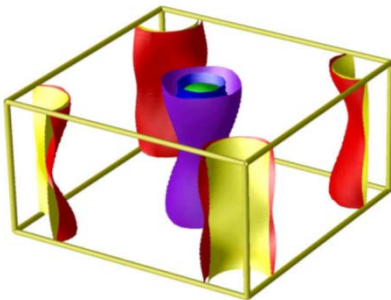
Phase sensitive experiments

A.A. Golubov and I.I. Mazin, *Appl. Phys. Lett.* **102**, 032601(2013)

Designing phase-sensitive tests for Fe-based SC's



h+ e-
h+ e-



h+ e-
e+ h-

h+ e-

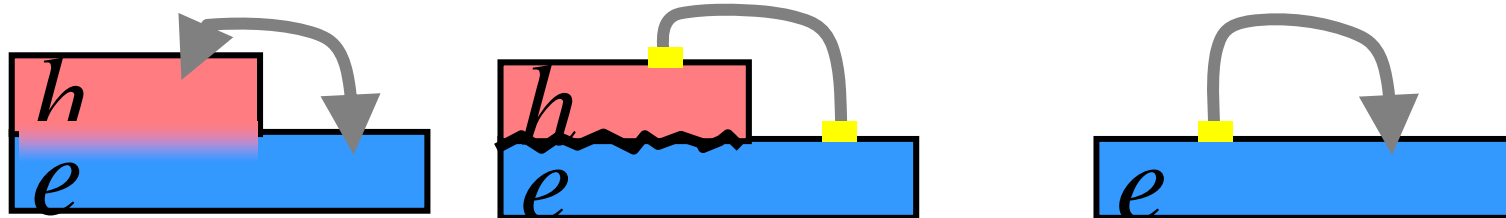
(a) Tunnel regime:

$$T_{\mathbf{k}} = \frac{4m_0^2 \hbar^2 K^2 v_L v_R}{\hbar^2 m_0^2 K^2 (v_L + v_R)^2 + (\hbar^2 K^2 + m_0^2 v_L^2)(\hbar^2 K^2 + m_0^2 v_R^2) \sinh^2(dK)}$$

The conductance is exponentially suppressed if $k_{\parallel}^2 / 2m_0 \lesssim 2(U - E_F)$.

(b) Point contact regime:

The conductance is angle-independent



h+ e-

h+ e-

h+ e-

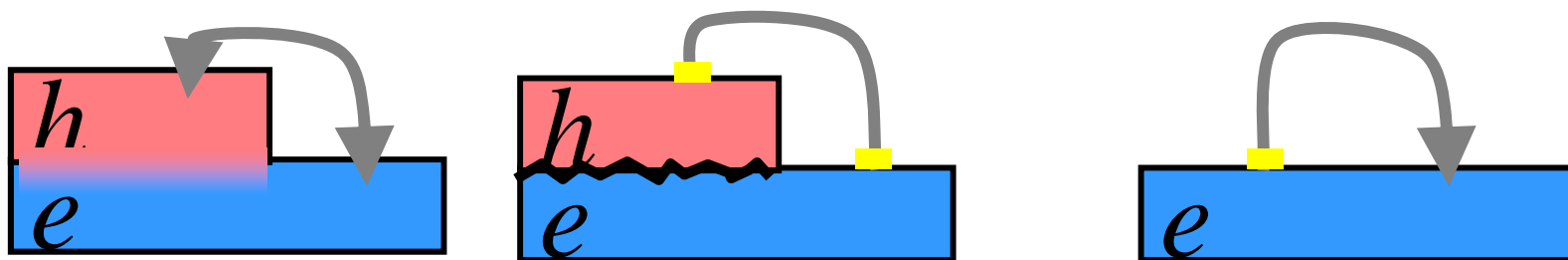
e+ h-

h+ e-

TABLE I. Three suggested designs for probing the relative phases of the order parameter in Fe-based superconductors. A tunneling barrier here is assumed to be thick enough to filter through the “tunneling cone” effect only the states near the zone center (holes), while a point contact is supposed to collect current in all directions and thus be dominated by the majority carriers. The sign of the order parameter is selected in such a way that the current through the left (upper) contact is always considered positive.

Design			
Fig. 1 panel	Left	Middle	Right
Upper/left contact	Point	Tunnel	Tunnel
Lower/right contact	Point	Tunnel	Point
Upper Δ_{hole}	-	+	+
Upper Δ_{elec}	+	-	-
Interface	Epitaxial	Rough	n/a
Lower Δ_{hole}	-	-	n/a
Lower Δ_{elec}	+	+	n/a
Upper contact current dominated by	Electrons	Holes	Holes
Lower contact current dominated by	Holes	Holes	Electrons

Golubov, Mazin,
APL **102**, 032601(2013)



h+ e-

h+ e-

h+ e-

e+ h-

h+ e-

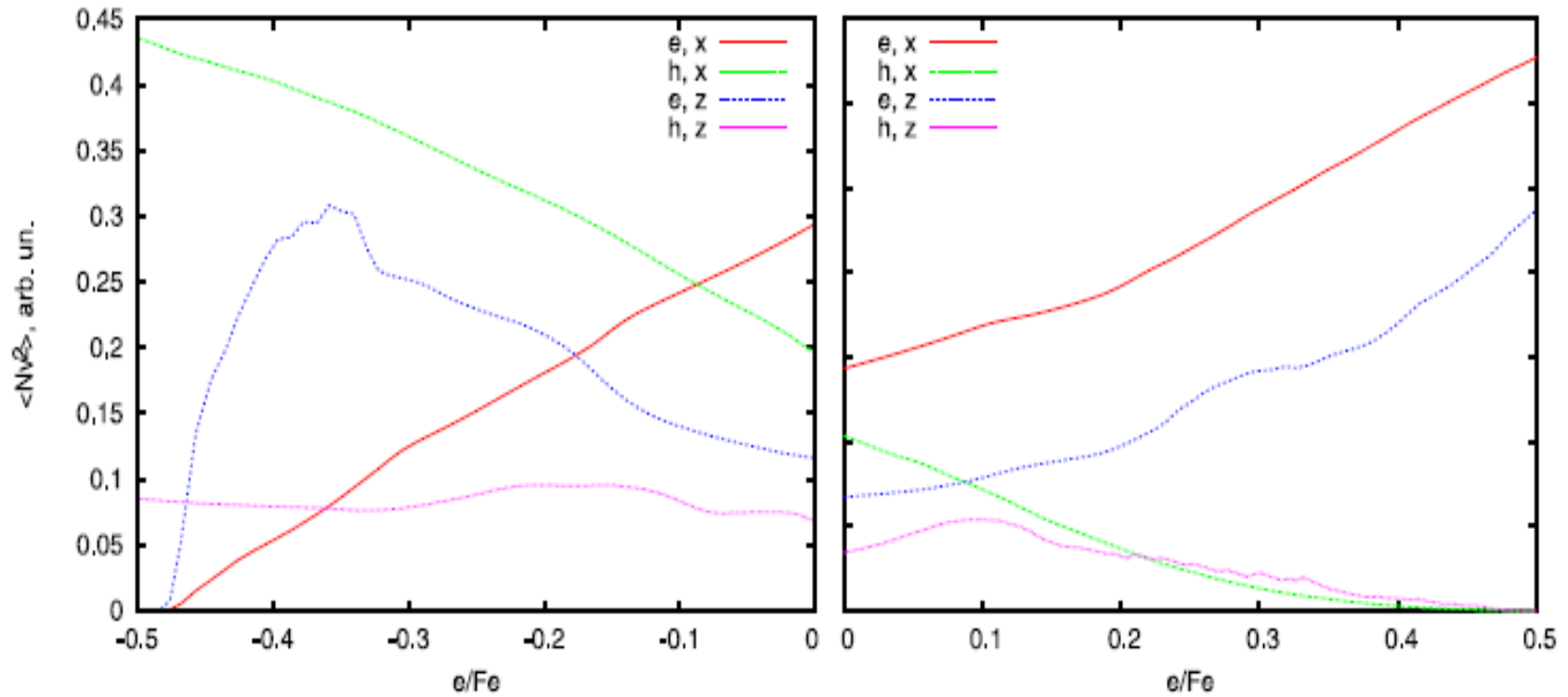


FIG. 2. Calculated transport function, $\langle N(E_F)v_F^2 \rangle$, for the hole-doped (left panel) and electron-doped (right panel) BaFe_2As_2 . Calculation for the electron-doped case was self-consistent in the virtual crystal approximation for the 10% Co doping and the rigid band approximation used around this composition. Similarly, the hole-doped composition was self-consistent for the 40% K doping and the rigid bands used thereafter.

Summary

- Impurity scattering: two regimes

- saturation of T_c to the **finite** value for $\langle \lambda \rangle_{FS} > 0$

- **critical impurity scattering** value for $\langle \lambda \rangle_{FS} < 0$

- With increasing strength of impurities there is transition $s_{+-} \longrightarrow s_{++}$ and T_c is stabilized.

Phys. Rev. B **84**, 180512 (2011); New J. Phys. **15**, 013002 (2013)

- **Phase sensitive experiments** may distinguish s_{+-} from s_{++} :
we have suggested experimental designs.

Appl. Phys. Lett. **102**, 032601(2013)

Further study: incorporation of microscopic boundary conditions
to evaluate Josephson current