Computation of atomic ionization and recombination properties in synchrotron and FEL radiation

S. Fritzsche Universität Oulu und GSI Darmstadt Moscow, 24th Mai 2012



Thanks to:

A.N. Grum-Grzhimailo, E. Gryzlova, N.M. Kabachnik, A. Surzhykov (theory)

R. Feifel, M. Meyer, T. Stöhlker and AP@GSI and others (experiment)

Deutsche Forschungsgemeinschaft DFG





Computation of atomic ionization and recombination properties in synchrotron and FEL radiation



4045508 Multiple ionization

Time-resolved ionization

Correlation pattern

11

21.0

Electron kinetic energy (eV)

14

Computation of atomic ionization and recombination properties in synchrotron and FEL radiation



Multiple ionization

Time-resolved ionization

Correlation pattern

Computation of atomic ionization and recombination properties in synchrotron and FEL radiation



- electron-photon vs. electron-electron interactions

Photoionization Autoionization



Radiative electron capture (REC) Dielectronic recombination (DR)





C. Brandau et al., PRL 100 (2008) 073201; PRL 89 (2002) 053201; PRL 91 (2003) 073202

- Dielectronic recombination (DR) process provides a unique tool for precise spectroscopy of HCI and, especially, doubly excited ionic states.
- Sensitive to nuclear, isotope and QED properties
- Interactions in intense (Coulomb) fields
- Great importance for plasma and FEL physics.

- finger prints upon magnetic and retarded interactions

K-LL DR into initially lithium-like ions:



N. Nakamura et al., PRL 100 (2008) 073203.

- finger prints upon magnetic and retarded interactions

K-LL DR into initially lithium-like ions:



Angular distribution of emitted photons



 $V_{ee} = V^{C} + V^{B} = \frac{1}{r_{12}}$ $+ \left(-\alpha_1 \alpha_2 \frac{\cos \omega r_{12}}{r_{12}} + (\alpha_1 \nabla_1)(\alpha_2 \nabla_2) \frac{\cos \omega r_{12}}{\omega^2 r_{12}}\right)$ only Coulomb Coulom + Breit M, = 0 M, = +1 $M_{1} = -1$ $M_{1} = -1$ M, = 0 M, = +1 $A_2 = -0.516$ $A_2 = +0.374$ $W(\theta) \propto 1 + \frac{A_2}{\sqrt{2}} P_2(\cos\theta)$

S. Fritzsche et al., PRL 103 (2009) 113001.

- finger prints upon magnetic and retarded interactions

K-LL DR into initially lithium-like ions:



Linear polarization of emitted photons



S. Fritzsche et al., PRL 103 (2009) 113001.



Z. Hu et al., PRL 108 (2012) 073002 (exp. confirmation).

Details matter:

-- Lyman-a vs. K-a emission from high-Z ions

(initially) bare ion

 $Ly-\alpha_1$ is strongly anisotropic

• 2p_{3/2}







Details matter: Adding one electron

-- Lyman-a vs. K-a emission from high-Z ions (initially) bare ion $2p_{3/2}$ (initially) H-like ion 2p_{3/2} 0.55 0.50 X. Ma et al, PRA 68 (2003) 042712. Ratio Ly $\alpha_1/Ly\alpha_2$ Ly- α_1 is strongly anisotropic 0.9 0.35 -U⁹²⁺ O-R at 102.0 MeV/u 0.8 U⁹¹⁺ 309 MeV/u 0.30 = 1-R at 116.6 MeV/u Intensity ratios for K α 1-S/K α 2-S $T_{p} = 102 \text{ MeV/u}$ 2-R at 124.9 MeV/u 0.7 0 30 60 90 120 150 180 3-R at 133.1 MeV/u observation angle θ [deg] 0.6 0.5 0.4 × Ŷ ¥ 0.3 0.2 0.1 20 0 80 40 60 100 120 140 160 180

 $K-\alpha_1$ is isotropic

Observation angle in Lab system (deg)

Details matter: Adding one electron

-- Lyman- α vs. K- α emission from high-Z ions



-- angular distribution as "observed" in experiments

$$\begin{split} W\left(\theta\right)_{K\,\alpha_{1}} &\sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta) & \text{A. Surzhykov et al., PRA 73 (2006) 032716.} \\ &= 1 + \left(N_{J=1} \frac{1}{\sqrt{2}} A_{2}(J=1) - N_{J=2} \sqrt{\frac{5}{14}} A_{2}(J=2)\right) P_{2}(\cos\theta) \end{split}$$

 $N_{J=1}$, $N_{J=2}$ relative populations of J=1, 2 states



-- for 220 MeV/u U⁹⁰⁺ ions following REC

$$W(\theta)_{K\alpha_{1}} \sim N_{J=1}W_{EI}(\theta) + N_{J=2}W_{M2}(\theta)$$

$$= 1 + (N_{J=1}\frac{1}{\sqrt{2}}A_{2}(J=1) - N_{J=2}\sqrt{\frac{5}{14}}A_{2}(J=2))P_{2}(\cos\theta)$$

$$= 1 + (N_{J=1}\frac{1}{\sqrt{2}}A_{2}(J=1) - N_{J=2}\sqrt{\frac{5}{14}}A_{2}(J=2))P_{2}(\cos\theta)$$

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-- following the Coulomb excitation of the projectiles

 $W(\theta)_{K\alpha_{1}} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$ A. Surzhykov et al., PRA 73 (2006) 032716. $=1+(N_{J=1}\frac{1}{\sqrt{2}}A_{2}(J=1)-N_{J=2}\sqrt{\frac{5}{14}}A_{2}(J=2))P_{2}(\cos\theta)$ 1.61.51.4excitation of 1.3He-like U⁹⁰⁺ ion 1.23 ntensity ratio Ko,/Ko, 1.111.0 Excited states of He-like heavy ions can be produced 0.9also by the Coulomb excitation of the projectile in the 0.80.7field of target atoms. 0.6 0.45 Experiments were already performed at the GSI storage D.4 ring for He-like uranium ions U⁹⁰⁺. D.D. 0.250 66 1210 • Strong anisotropy of the subsequent Ka, radiation has observation angle [0108]

been observed!

-- following the Coulomb excitation of the projectiles

$$W(\theta)_{K\alpha_{1}} \sim N_{J=1} W_{E1}(\theta) + N_{J=2} W_{M2}(\theta)$$

= 1 + (N_{J=1} \frac{1}{\sqrt{2}} A_{2}(J=1) - N_{J=2} \sqrt{\frac{5}{14}} A(J=2)) P_{2}(\cos \theta)

 $N_{J=1}$, $N_{J=2}$ relative populations of J=1, 2 states



- Angular distribution results dominantly from the decay of the J=1 level.
- Role of electron-electron interactions still unexplored.



Techniques and tools for strong-field processes

- to describe the structure & dynamics of atoms and ions

Multiconfiguration expansions

$$\psi_{\alpha}(PJM) = \sum_{r}^{n_{c}} c_{r}(\alpha) \gamma_{r} PJM >$$

Construct a `physically motivated' basis in the N-electron Hilbert space.



Many-particle character "electronic correlations"



Relativistic effects

Shell structure static vs. dynamic correlations

Direct vs. indirect effects QED corrections

Generalization of the knowledge about (Dirac's) one- and few-electron atoms in such a way to enable the "computation" of complex systems and processes.

Techniques and tools for strong-field processes

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Shell structure static vs. dynamic correlations

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Energies & Wave functions

- Cowan / CIV3
- MCHF
- GRASP(-92) / RATIP
- "Desclaux"
- Coupled-Cluster

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S. Fritzsche, JESRP 114-116 (2001) 1155; Comput. Phys. Commun. 183 (2012) 1525

RATIP

Relativistic Atomic Transition, Ionization and Recombination Properties

010 010

AUGER: Auger rates, relative intensities, angular distribution & spin polarization parameters.

CESD: Determinant representation of atomic and configuration state functions.

Many-electron basis (wave function expansions)

- Construction and classification of N-particle Hilbert spaces
- Shell model: Systematically enlarged CSF basis
- Interactions
 - Dirac-Coulomb Hamiltonian
 - Breit interactions + QED
 - Electron continuum; scattering phases
- Coherence transfer and Rydberg dynamics

REC: Radiative recombination & electron capture rates, angular parameters.

RELCI: Relativistic configuration interaction wave functions & QED estimates.

REOS: Relaxed-orbital Einstein A and B coefficients, transition probabilities and lifetimes.

TOOLBOX: Level energies and notations; manipuations of file interfaces, miscelaneous.

COULOMB: Exitation amplitudes, (M_J-dependent) cross sections, alignment parameters.

S. Fritzsche, JESRP 114-116 (2001) 1155; Comput. Phys. Commun. 183 (2012) 1525

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Multiple ionization of noble gases

-- using magnetic bottle techniques



P. Kruit and F. H. Read, J. Phys. E <u>16</u>, 313 (1983) J. H. D. Eland et al, Phys. Rev. Lett. <u>90</u>, 053003 (2003)

Advantages

- Electron detection with high sensitivity and resolution (especially charge-particle detect.)
- Supports both, normal TOF but also zero-kinetic energy (resolution)
- High collection efficiency (reconstruction of 3D velocity distributions)
- Coincidence maps: Differential analysis of outgoing electrons
- Easy to combine with atomic and molecular beams
- ☆ No information about angular distribution and spins of photoelectrons

Multiple ionization of noble gases @ synchrotrons

-- coincidence techniques using a magnetic bottle

 $Kr \rightarrow Kr^{3+}$

Double Auger decay of 3d-ionized krypton

- Coincidence on 3d photo electron as first arrival electron.
- Six stripes arise from combination of 3d hole states and the ⁴S, ²D and ²P finals states of Kr³⁺ 4p⁻³
- Dark spots refer to Auger lines.



E. Andersson et al, PRA 82 (2010) 043418.

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Calculations helped identify new levels and decay pathes in the sequential (auto-) ionization.



- via core-valence doubly ionised intermediate states



Single photon core-valence double ionisation Spectra of krypton recorded at hv = 150 eV.



E. Andersson et al, PRA 82 (2010) 043418; PRA 85 (2012) 032502.

- via core-valence doubly ionised intermediate states



- via core-valence doubly ionised intermediate states



Features of the ab-initio approach

- Combines time-independent density matrix with proper construction of `two-electron' ionization amplitudes.
- Coupling of wave packets from discretization of the one-electron spectrum.
- Two-electron continuum through direct diagonalization (damped CI vs. finite e-e interaction with r_{cut}).
- Explicit summation over intermediate many-electron states (continua).

- via core-valence doubly ionised intermediate states



Approach works well:

- + if DI is insensitive with regard to energy sharing
- + core-core and core-valence ionization (localized electron density)
- + reasonably high photon energies
- more details desirable about energy sharing and angular dependence
- more multi-electron spectra, other elements and shell structures.

Light-matter interactions at increased (FEL) intensities

- first non-linear studies on electron emission

Details in the ionization dynamics of electrons became visible first in the sequential and direct DI of nobles gases





Collaboration with A. Grum-Grzhimailo, E. Gryzlova & N. Kabachnik

Two-photon double ionization (TPDI)

-- sequential vs. direct knockout of several electrons



Depolarization due to multiple (auto-) ionization – exotic matter states with multiple inner-shell holes

Quantum evolution of the density operator:



Depolarization due to multiple (auto-) ionization

- interplay of different time scales leads to depolarization

Quantum evolution of the density operator:

$$\rho_{kq}(J, J'; t) = \rho_{kq}(J, J'; t_1) \exp[(i\omega_{JJ'} - \Gamma_{JJ'})(t - t_1)]$$

$$\boxed{\underbrace{\vdots}} J, J'$$

where
$$\omega_{JJ'} = E_J - E_{J'}$$
 $\Gamma_{JJ'} = (\Gamma_J + \Gamma_{J'})/2$

Depolarization factor in the e-e correlation function

$$h(J,J') = \int_{-\infty}^{+\infty} dt_1 \ I(t_1) \int_{t_1}^{\infty} dt_2 \exp[(i\omega_{JJ'} - \Gamma_{JJ'})(t_2 - t_1)] \ I(t_2)$$





"JPB Highlight 2011"

Depolarization due to multiple (auto-) ionization – non-linear response to intense ultra-short x-rays

Quantum evolution of the density operator:

$$\rho_{kq}(J, J'; t) = \rho_{kq}(J, J'; t_1) \exp[(i\omega_{JJ'} - \Gamma_{JJ'})(t - t_1)]$$

0.10

0.06 0 0.06 0.04 0.02



where
$$\omega_{JJ'} = E_J - E_{J'}$$
 $\Gamma_{JJ'} = (\Gamma_J + \Gamma_{J'})/2$



L. Young et al., Nature 466 (2010) 56.

To proceed beyond `rate-equation' dynamics in understanding the femto-second electronic response of atoms in strong fields.





G. Doumy et al., PRL 106 (2011) 083002.

Depolarization due to multiple (auto-) ionization non-linear response to intense ultra-short x-rays

Quantum evolution of the density operator:

$$\rho_{kq}(J, J'; t) = \rho_{kq}(J, J'; t_1) \exp[(i\omega_{JJ'} - \Gamma_{JJ'})(t - t_1)]$$
where $\omega_{JJ'} = E_J - E_{J'}$ $\Gamma_{JJ'} = (\Gamma_J + \Gamma_{J'})/2$

1110



Coherent time evolution of inner-shell excited systems – in short-pulse or pump-probe experiments

Explicitly time-dependent density operator:



Coherent time evolution of inner-shell excited systems – in short-pulse or pump-probe experiments

Explicitly time-dependent density operator including spatial degrees of freedom:

$$\dot{\rho} = \frac{i}{\hbar} [H, \rho] + L\rho$$
Based Liouville's equation
$$i\frac{d\rho_{kq}(\alpha, \beta)}{dt} = \sum_{\kappa'q'} \sum_{\gamma} \left\{ F_{\kappa q}^{\kappa'q'}(\alpha, \beta, \gamma, \frac{\text{pulses}}{\text{geometry}}; t) \rho_{k'q'}(\gamma, \beta) \quad \text{direct coupling}$$
Atomic (transition & ionization)
amplitudes from many-body
theory (RATIP)
S. Fritzsche, CPC 183 (2012) 1525
$$-i\Gamma_{\kappa q}^{\kappa'q'}(\alpha, \beta, \gamma; t) \rho_{k'q'}(\gamma, \beta) \right\}$$
ionization & ioniza

Collaboration with Alexei Grum-Grzhimailo

Coherent time evolution of inner-shell excited systems – in short-pulse or pump-probe experiments

Explicitly time-dependent density operator including spatial degrees of freedom:



Summary

- Intense FEL pulses lead to "hollow atoms" and ions, i.e. extreme matter in a truly exotic form. Dynamics of strongly correlated electrons in controlled light fields is a presently emerging field and require the coherent time evolution of the systems.
- For atoms & molecules, multiphoton ionization and autoionization is likely the first non-linear x-ray phenomenon that will be explored in good qualitative and quantitative detail, i.e. shows the predictive power of theory.

Summary

- Intense FEL pulses lead to "hollow atoms" and ions, i.e. extreme matter in a truly exotic form. Dynamics of strongly correlated electrons in controlled light fields is a presently emerging field and require the coherent time evolution of the systems.
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Two main avenues towards real quantum dynamics:

... to describe (time-dependent) ionization dynamics of strongly coupled systems

"Wave-packet dynamics": Solution of time-dependent Schrödinger equations

(atomic/molecular physics approach)

Coherent state evolution: Generalized Bloch-type equations
 (quantum optical approach)

Summary ... and where to go ?

- Intense FEL pulses lead to "hollow atoms" and ions, i.e. extreme matter in a truly exotic form. Dynamics of strongly correlated electrons in controlled light fields is a presently emerging field and require the coherent time evolution of the systems.
- For atoms & molecules, multiphoton ionization and autoionization is likely the first non-linear x-ray phenomenon that will be explored in good qualitative and quantitative detail, i.e. shows the predictive power of theory.
- Ionization and recombination are indeed fundamental for discovering new phenomena and for obtaining a quantitative understanding of light-matter interactions, both in strong-fields physics and many-particle dynamics.